

PUBLIC AND PARENTAL INVESTMENTS AND CHILDREN'S SKILL FORMATION

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Public and Parental Investments, and Children's Skill Formation

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Abstract

This paper studies the interaction between parental and public inputs in children's skill formation when families can sort into public institutions with different quality. We show theoretically that the effects of public investments depend on the elasticity of substitution between inputs made at home and in institutions. Using an RCT that increased public preschool quality, we test the main model implications. We find that improved preschool quality leads to heterogeneous parental responses, which mediate the longer-run effects on children's skills. We show that these responses are only compatible with inputs made at home and in institutions being substitutes.

JEL Classification: I24, I28, I21, J24.

Keywords: skill formation, parental time investments, public investments, school quality

1 Introduction

The importance of the childhood environment for shaping opportunities later in life is well established (e.g., [Heckman, 2006](#)), and a large literature has documented effects of early childhood investments on skills and adult outcomes such as income, education, health, and crime, for example, by studying the effects of childcare enrollment (e.g., [Cascio and Schanzenbach, 2013](#); [Cornelissen et al., 2018](#); [Fort et al., 2020](#); [Havnes and Mogstad, 2011](#)). However, an equally important margin today is the *quality* of childcare, as the preschool attendance rate of 3 to 5 year-olds in the OECD is almost 90%.¹ Yet, much less is known about the effects of childcare quality, and how these out-of-home investments interact with the investment decisions parents make at home.

In this paper, we seek to fill this void by studying how children’s skill formation is affected by the interaction between parental investments and public investments in the quality of institutions. We investigate this both theoretically and empirically.

The paper first presents a general model of child skill formation where investments are made both at home and in institutional settings (e.g., preschools and schools), whose quality may be influenced both by public investments and by parents through sorting. We link this model to survey and register data for children who were part of a randomized controlled trial that increased preschool quality through a program that significantly improved preschool-teachers’ training of language and (pre-)literacy skills. The survey measures and administrative register data allow us to assess parental investments, school choice, and children’s later outcomes. The empirical setting focuses on children aged 3 to 9 years in Denmark. We interpret the treatment effects and parental responses through the lens of the model, which allows us to go a step further than simply to state whether public investments crowd out parental ones, or whether parents meet increased public quality by also intensifying their own investment activities. Instead, the model allows us to nonparametrically identify whether

¹Average preschool enrollment at age 3 to 5 years is 90% in the EU, 60% in the U.S., and 87% for all OECD countries ([OECD, 2019](#), Table B2.2).

the two types of investments are substitutes or complements in the skill production function with a minimal set of assumptions.

We present three main results. First, the model shows that the extent to which an increase in public investments actually boosts overall investments (and thus child skills) depends on how parents respond and whether inputs made at home and in institutions are complements or substitutes. This elasticity of substitution is given by the relative marginal productivities of parents' time spent either investing at home or influencing institutional quality via sorting, which in turn depend on the specific underlying home and education production functions. This result is very general, as it holds without any functional forms imposed on investment or production functions in the model.

Second, the RCT shows that increasing the quality of childcare reduces skill gaps (measured by language test scores) between children from disadvantaged and affluent backgrounds. For children whose parents have a high school degree or less as highest education, test scores remain 0.26 standard deviations higher in the treatment group than in the control group at ages 8 to 9 years (4 to 5 years after the intervention). In contrast, there are no treatment effects at ages 8 to 9 for children whose parents have at least a college degree. The playing field is leveled, however, only due to differences in how parents respond to the change in institutional quality. High-skilled parents generally invest more in their children's skill formation than low-skilled parents (both at home and via sorting into better institutions), but the intervention leads low-skilled parents to significantly increase home inputs while high-skilled parents mainly "consume" some of the public investment (provided from the treatment) by reducing their efforts put into sorting.²

Third, our model predictions show that the parental responses we find are only compatible with home and institutional investments being substitutes. We show that the intervention

²We document substantial sorting in schools both by both families *and teachers* (as also found in [Pop-Eleches and Urquiola, 2013](#)). We show that Danish public schools (a school system where expenses in each school are equalized based on substantial redistribution of local area tax-revenue as opposed to e.g., schools in the U.S.) are not only characterized by clustering of children from at-risk families and affluent families, teachers also sort based on the student body. Thus, the most able teachers are most likely to work in schools with children from affluent backgrounds.

works as a progressive transfer increasing the low-skilled parents' utility most, even when one factors in parental responses where affluent parents utilize the higher public investments to adjust their time inputs in their children's skill formation.

This paper expands earlier models of child skill development and parents' investments and provides an empirical test of the model's central relationships through a RCT.³ We are the first to formulate and provide empirical evidence for a model that separates investments made at home and in institutions while i) allowing substitution or complementarity between these two types of inputs, ii) allowing parents to affect institutional quality by sorting into higher quality neighborhoods and better preschools or schools, and iii) including parents' labor supply decisions in the trade-off between allocating time to leisure, time at home with children, and work. We are also among the first studies to use a RCT to provide insights into the parameters of a child skill formation model (see also [Attanasio et al., 2020](#); [Chaparro et al., 2020](#)). Importantly, our paper's findings rest on a minimal set of assumptions both in the model and empirically where we address central questions about the skill production function using simple mean-differences between the treatment and control groups.

We thereby complement the influential studies by [Becker and Tomes \(1986\)](#), [Cunha and Heckman \(2007\)](#), and later extensions that estimate human capital production functions including parents' investments and labor supply decisions ([Attanasio et al., 2020](#); [Bernal and Keane, 2010](#); [Del Boca et al., 2014](#); [Gormley et al., 2008](#)), school inputs and skill development ([Nicoletti and Rabe, 2014](#)), socio-emotional development ([Moroni et al., 2019](#)), children's own investment decisions ([Del Boca et al., 2019](#)), and how mothers trade off the quantity and quality of maternal and non-maternal care against their own labor supply ([Chaparro et al., 2020](#)). Our model also relates to [Fort et al. \(2020\)](#), who study children's skill formation in a context of heterogeneous childcare quality offers, and who also let parents trade off time in the market with time spent at home.

³The baseline model takes a general setup with a minimum set of assumptions. But once we impose functional form assumptions about child skill production (a CES technology) later in the paper, the model becomes an extension of the skill formation model by [Cunha and Heckman \(2007\)](#).

In addition, we add to the literature that studies how parents respond to changes in the quality of public investments in children, and reconcile the puzzle that previous studies come to different conclusions regarding whether parents behave as if home and institutional inputs are complements or substitutes (see a discussion in [Rabe, 2019](#)). On the one hand, [Gelber and Isen \(2013\)](#) find that randomization into the higher-quality Head Start increases parental involvement (interpreted as complementarity) but also reduces parental expenses on childcare.⁴ On the other hand, [Fredriksson et al. \(2016\)](#) find that children are more likely to be moved to a different school and those with high-income parents receive more help with homework when class size increases, and [Pop-Eleches and Urquiola \(2013\)](#) similarly find that school-quality and help with homework are inversely related (interpreted as the home and institutional inputs being substitutes). Our model highlights that whether the components are substitutes or complements cannot be answered by considering a single adjustment in isolation. Instead, one has to consider the relative adjustments to parental inputs at home and sorting effort to determine whether they are substitutes or complements.

Moreover, by studying how family background moderates the effects of increasing the quality of universal childcare, our empirical findings and model predictions add to the large body of research into the effects of universal childcare on later outcomes (e.g., [Baker et al., 2008](#); [Cascio and Schanzenbach, 2013](#); [Cornelissen et al., 2018](#); [Datta Gupta and Simonsen, 2010, 2012](#); [Havnes and Mogstad, 2011, 2015](#)). While programs such as universal childcare may have heterogenous effects due to different counterfactuals (e.g., the quality of parental care), our findings also show that effects may differ across family background due to the trade-offs parents face between spending time with the child (thereby increasing inputs at home) or at work (increasing consumption but also facilitating residential sorting through

⁴Related, [Chang et al. \(2020\)](#) find that highly educated parents increase their financial investments in reaction to being exposed to a higher-quality teacher, but slightly reduce their time investments. [Bonesrønning \(2004\)](#) finds that Norwegian parents reduce the time spent with their children on homework when class size increases.

increased income).⁵

Finally, we also complement the studies that illustrate how the effects of policies such as Head Start are mediated by sorting and school quality (Ansari and Pianta, 2018; Currie and Thomas, 2000; Johnson and Jackson, 2019; Lee and Loeb, 1995). We show substantial differences in the quality of institutions and sorting exist, even in a country such as Denmark where inequality in disposable income is low compared to most other countries and institutions' budgets are equalized by the Danish welfare state.

The paper progresses as follows: Section 2 presents the model of skill formation that includes both parental and public investments, while taking both parents' labor supply decisions and sorting into account. Section 3 relates the model to the empirical setting of Danish preschools and schools, and introduces the RCT. Section 4 describes the data and presents balancing tests confirming the randomization procedure. Section 5 presents the main empirical findings and Section 6 concludes.

2 Framework

We first outline our theoretical framework and then study how total investments in children are a function of parents' choices of home investments and institutional sorting. This section focuses on the key relations. Appendix B presents model derivations in detail.

2.1 A Technology of Skill Formation with Home and Institutional Investments

We begin with a general model of skill formation across childhood, where a parent makes investment decisions maximizing their own utility, which is increasing in their child's skills. Skills evolve from period to period such that end-of-period skills θ_t are a function of past

⁵Our result that institutional investments also benefit high-SES families because high-SES parents have higher opportunity costs of providing home investments echoes the finding in Cornelissen et al. (2018); Kline and Walters (2016) that potential gains from program take-up and the take-up probability are inversely related.

skills (θ_{t-1}) and the current period’s investments I_t .⁶

$$\theta_t = j(\theta_{t-1}, I_t) \tag{1}$$

We next implement this paper’s central notion: children’s skill development is not only the target of direct parental inputs at home but also of inputs in out-of-home settings. To capture this effect, we define “total investments” I_t as a composite of two underlying investment types: those made at home by parents P_t , and those made in an institutional setting G_t (e.g., preschool and school):

$$I_t = m(P_t, G_t) \tag{2}$$

This general framework fits in essence the canonical model outlined in [Becker and Tomes \(1986\)](#) with the multiperiod skill formation and investments as in [Cunha and Heckman \(2007\)](#), with one important conceptual difference (expanded upon below): parents determine home inputs but also the quality of institutions through sorting.

To have a common unit, we consider all parental decisions to relate to their *time use*. Parental home-investments P_t are a function of their time spent directly with their child (x_t), where the quality of input time may vary with parents’ skills, θ_P (see e.g., [Cobb-Clark et al., 2019](#); [Doepke and Zilibotti, 2017](#)). Institutional investments G_t are given by three inputs:⁷

1) There is a baseline public investment yielding an institutional quality, \underline{G} , throughout the education system, including preschool.⁸ The baseline could, for example, be given by

⁶Skills in period zero are a function of parental skills θ_P and in-utero investments I_0 : $\theta_0 = j(\theta_P, I_0)$. Skills θ_t could be a vector of several types of skills. For simplicity, we here only consider one type of skills as a scalar in the framework, as our empirical section focuses on language skills.

⁷We focus on institutional quality from the parents’ perspective when deciding where to send their child. A large literature has studied inputs in the education production function (see e.g., [Hanushek, 2002](#), for a review) affecting child skills, including peer and teacher quality, class sizes, etc. We do not study this relationship. But, as we will describe in the following, imposing assumptions about the elasticity of substitution between P and G implicitly imposes assumptions about the education production function.

⁸We do not consider the funding of \underline{G} here, but we return to this in Section 5.3.

national guidelines.

2) Within this overall national level, institutional quality may vary on the regional or local level. Parents can influence the institutional quality their child is exposed to by choosing where to live. Neighborhood level institutional quality, or neighborhood public goods, are associated with rent levels and real estate prices; institutional quality thus is positively correlated with parental income.⁹ Parental wage income Y_t is a function of their labor supply h_t and their hourly wage rate $w(\theta_P)$. Parents take the wage rate as given, and income equals $Y_t = h_t w$. Parents spend fraction κ of Y_t on residential choice.

3) We include a third input, e_t , to institutional investments: the time parents spend on school sorting within their neighborhood (e.g., visiting schools, contacting administrative personnel, volunteering for after-school activities), as we empirically observe that even for a given residential choice, there are typically several potential institutions that children can attend.¹⁰ Including this time spent on sorting as an input that does not directly affect consumption (in contrast to labor supply) implies that it has the same opportunity costs in terms of foregone leisure as time spent on home-investments (x_t). The input e_t thereby allows us to distill the intuition in parents' trade-off when balancing investments through time with children at home against investments through sorting (time away from home).¹¹

⁹Black (1999), for example, shows a strong link between housing prices and local schools. We do not model general equilibrium effects of sorting and neighborhood-specific public goods as do Epple and Romano (1998) and Bayer et al. (2007), and we also abstain from directly modeling mechanisms such as peer effects (described in e.g., Blume et al., 2011; Epple and Romano, 2011) and the multidimensionality of schools' effects (Jackson and Beuermann, 2019).

¹⁰Walters (2018) analyzes sorting into charter schools in the U.S. and how non-pecuniary sorting-mechanisms shape the type of children who are enrolled. In the Danish case that we use for our empirical focus, there is free school choice as long the school alternative has vacant slots. Public school slots go first to children who live within the school attendance boundaries. Bjerre-Nielsen and Gandil (2020) show that even when attendance boundaries for public schools are re-drawn, high-resource parents often defy reassignments to schools they perceive as lower quality. Thus, even when the governing municipalities assign children to specific schools, parents are effectively able to choose other schools. In other countries where catchment areas are strongly enforced according to residential area, parental sorting may be limited to choice of residence. This would have e drop out of the model, but the model's main predictions would be qualitatively similar.

¹¹To see this, note that in equilibrium (taking $t = 2$ as an example) parents set their time use such that: $\frac{\partial u_2}{\partial l_2} = \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial l_2} \frac{\partial l_2}{\partial P_2} \frac{\partial P_2}{\partial x_2} = \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial l_2} \frac{\partial l_2}{\partial G_2} \frac{\partial G_2}{\partial e_2} = \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial l_2} \frac{\partial l_2}{\partial G_2} \frac{\partial G_2}{\partial h_2} + \frac{\partial u_2}{\partial c_2} w(1 - \kappa)$ where the final term $\frac{\partial u_2}{\partial c_2} w(1 - \kappa)$ captures labor supply's effect on consumption. β is a discount factor. V is parents' valuation of child skills.

Taken together, the components of investments become

$$\begin{aligned} P_t &= p(x_t, \theta_P) \\ G_t &= g(\underline{G}, \kappa Y_t, e_t, \theta_P), \end{aligned} \tag{3}$$

where we assume that $P()$ and $G()$ are increasing in all of their inputs. Parents thus spend their time on work (h_t), leisure (l_t), investing in children directly (x_t), and on institution choices within the neighborhood (e_t). Their total time is allocated as $1 = h_t + l_t + x_t + e_t$. Thus, parents need to balance the time spent at home with their children against their own leisure, sorting effort, and hours worked.

We consider two periods of skill formation where parental utility is directly derived from own consumption and leisure, and indirectly from children's future skills θ_2 . All periods are discounted at factor β . We initially assume that parents have no access to borrowing, but the main conclusions carry through regardless of credit opportunities. Parents' optimize:

$$\max U(c_1, c_2, l_1, l_2, \theta_2) = u(c_1, l_1) + \beta u(c_2, l_2) + \beta^2 V(\theta_2) \tag{4}$$

subject to production functions in Eqs. (1) to (3) and budget constraints.

2.2 Equilibrium Conditions and the “Production” of Investments

The optimization of this very general problem yields a set of revealing equilibrium conditions (all first order conditions are shown in Section B.1). Parents equalize the marginal productivities of investing directly in their child at home (x_t) or indirectly via sorting (e_t):

$$\frac{\partial I_t}{\partial P_t} \frac{\partial P_t}{\partial x_t} = \frac{\partial I_t}{\partial G_t} \frac{\partial G_t}{\partial e_t}, \quad \text{for } t \in \{1, 2\} \tag{5}$$

Hence, when parents allocate their time optimally, they are indifferent between spending marginally more time investing in children's skills at home (e.g., reading with the child)

and through sorting into better institutions. While this may seem like standard first order conditions, Eq. (5) holds important implications. To see this, a slight re-arrangement yields:

$$|\text{MRTS}(P_t, G_t)| = \frac{\partial I(P_t, G_t)/\partial P_t}{\partial I(P_t, G_t)/\partial G_t} = \frac{\partial g(\underline{G}, \kappa Y_t, e_t, \theta_P)/\partial e_t}{\partial p(x_t, \theta_P)/\partial x}, \quad t \in \{1, 2\} \quad (6)$$

The equation states that the marginal rate of technical substitution (MRTS) between home and institutional components of total investments in skill formation (i.e., the rate one component must increase to keep total investments constant when the other component decreases) must equal the ratio between the marginal productivities of parents' time spent with their children and time spent influencing institutional quality.¹² The elasticity of substitution between home and institutional investments is given by:

$$\varepsilon_{P,G} = \left[\frac{\partial \text{MRTS}(P, G)}{\partial (P/G)} \frac{P/G}{\text{MRTS}(P, G)} \right]^{-1} \quad (7)$$

The second term of this product will always be positive. Therefore, whether P and G are substitutes or complements in the “production” of investments (whether $\varepsilon_{P,G}$ is positive or negative) depends on the sign of the first term, which relates a change in the MRTS to an underlying change in the ratio of investments made at home and in institutions (P/G).¹³ Hence, the consequences for total investments when public investments increase depend on whether the home and institutional components are substitutes or complements.

Therefore, a test for whether home-investments and institutional investments are substitutes or complements is not simply given by considering how one of the two changes when public investments vary, as suggested in, for example, [Fredriksson et al. \(2016\)](#), [Pop-Eleches and Urquiola \(2013\)](#), or [Gelber and Isen \(2013\)](#), who consider how parents adjust one margin of investments when institutional quality varies. The answer depends on how parents

¹²Thus, parents' investment decision essentially corresponds to the textbook case where a profit-maximizing firm producing $Y = F(K, L)$ from capital K and labor L will choose inputs such that $-\text{MRTS} = \frac{\partial Y/\partial L}{\partial Y/\partial K} = w/r$.

¹³See Section [B.1](#) for further derivations and discussion of the intuition behind this result.

jointly adjust inputs affecting home and institutional quality. Eq. (5) also highlights the crucial role of assumptions about how P_t and G_t interact in producing overall investments I_t : These assumptions about the higher-level or outer function of I_t have immediate implications for the micro-foundations or inner functions $p()$ and $g()$. The “outer” and “inner” parts of the production functions are inherently linked. For example, assuming a Cobb-Douglas or CES production technology for I_t , not only shapes $\frac{\partial I_t}{\partial P_t} / \frac{\partial I_t}{\partial G_t}$, but it also imposes implicit assumptions about institutional environments and the specific form of education production function as well as the functional form of family interactions at home.

2.3 Specific Model: Residential Choice and Functional Forms

The previous discussion is based on the most general version model that applies to many settings. To be able to derive explicit predictions of the model, we next introduce three alterations (Sections B.2 and B.3 provide detailed derivations): Borrowing,¹⁴ a constraint to residential choice (to illustrate how sorting influences parental time use across the childhood), and specific functional forms in the production functions (to provide an empirical test of whether home and institutional inputs are complements or substitutes).

The general model allows parents to optimize their residential choice every period. Yet this is not observed in practice. Instead, we note that the vast majority of parents choose where to live before their child starts school, and then remain there throughout the child’s compulsory schooling (see Section 5.2 and Fig. A.1). We model this stickiness by having parents’ residential choice as a function of fraction κ of their income early in the child’s life, so that residential quality for both periods is determined by $\kappa Y_1 = \kappa h_1 w(\theta_P)$.

This lock-in of early residential choices, together with unlimited borrowing at the discount rate between periods 1 and 2, generates intertemporal differences in the marginal returns to

¹⁴Allowing for borrowing facilitates a direct comparison of the intertemporal allocation of investments in our model with those in, for example, Cunha and Heckman (2007). But as we focus on how parents react in the second (and last) period of the two-period model, they cannot re-optimize their borrowing behavior in the absence of leaving negative bequests in any case. Therefore, the assumption of borrowing is not consequential here.

parental investments.¹⁵ Across periods, parents optimally allocate their time uses as:

$$\frac{\partial \theta_2}{\partial x_1} = \frac{d_w}{\beta} \frac{\partial \theta_2}{\partial x_2} \quad (8)$$

$$\frac{\partial \theta_2}{\partial e_1} = \frac{d_w}{\beta} \frac{\partial \theta_2}{\partial e_2} \quad (9)$$

$$\frac{\partial u_1}{\partial l_1} = \frac{d_w}{\beta} \frac{\partial u_2}{\partial l_2} \quad (10)$$

where $d_w = \frac{(\beta\kappa w + (1-\kappa) - \beta\kappa)}{(1-\kappa w)}$ is a term that depends on fixed parameters as well as the parental wage rate $w(\theta_P)$, and is increasing in θ_P . d_w implies that — because children’s longer run skill development depends on residential choices early in the childhood — parents will dedicate more time to sorting (and work) and less time to child-related activities and leisure when the child is young compared to the case without constraints on moving.

When studying in greater detail how parents react to changes in the quality of institutions, the specific interactions between types of parental investments become crucial. Therefore, we continue with functional forms for the production functions. We assume that skills and investments follow a nested CES-structure over the two periods (see derivations in Section B.3). Note that this structure does not require a positive or negative elasticity of substitution and therefore remains flexible. Children’s skill formation is given by:

$$\theta_t = [\gamma \theta_{t-1}^\phi + (1 - \gamma) I_t^\phi]^{1/\phi}, \quad t \in \{1, 2\} \quad (11)$$

The parameter γ captures the effect of self-productivity (skills beget skills, [Cunha et al., 2006](#)), and $(1 - \gamma)$ reflects the importance of investments made in period t .¹⁶ The elasticity of substitution between the different inputs in the skill formation is given by $\frac{1}{1-\phi}$. The inputs will be perfect substitutes if $\phi \rightarrow 1$ and perfect complements as $\phi \rightarrow -\infty$.

¹⁵Note that we obtain specific relationships of marginal productivities over time when introducing an additional assumption that the marginal productivities of parental time in generating institutional investments, via school choice and labor supply, are proportional (such as $\kappa w \cdot \partial g / \partial e_t = \partial g / \partial h_t$). This can be obtained without specific functional form assumptions: see Eqs. (B.30) to (B.32) in Section B.3.

¹⁶This setup simplifies [Cunha et al. \(2010\)](#) as we consider a time invariant elasticity of substitution.

The inner part of the model — the “production” of total investments — is given by:

$$I_t = [\pi P_t^\sigma + (1 - \pi)G_t^\sigma]^{1/\sigma}, \quad t \in \{1, 2\} \quad (12)$$

where the elasticity of substitution between home and institutional inputs is given by $\frac{1}{1-\sigma}$, while π defines the relative importance of the two components. The inputs will be perfect substitutes if $\sigma \rightarrow 1$ and perfect complements as $\sigma \rightarrow -\infty$.

Furthermore, we assume that the underlying production functions take the form $f(x_t, \theta_P) = (x_t \theta_P)^a$ and $g(\underline{G}, \kappa Y_1, e_t, \theta_P) = (\underline{G} + \kappa w h_1 + e_t)^b$, where $0 < a, b < 1$.¹⁷ The ratio of early to late investments in private and institutional settings becomes:

$$\frac{x_1}{x_2} = \left[\frac{\underline{G} + \kappa w h_1 + e_1}{\underline{G} + \kappa w h_1 + e_2} \right]^{\frac{1-b\sigma}{1-a\sigma}}. \quad (13)$$

If we further — for expositional purposes — align the functional form of investments in private and public by setting $a = b$, the full production function can be expressed as:

$$\theta_2 = \left\{ \gamma^2 \theta_0^\phi + \gamma(1 - \gamma) \left[H(\theta_P) x_1^a \right]^\phi + (1 - \gamma) \left[H(\theta_P) x_2^a \right]^\phi \right\}^{1/\phi} \quad (14)$$

where $H(\theta_P) = \theta_P^a \pi^{\frac{1}{\sigma}} \left[1 + \frac{\pi}{(1-\pi)} \frac{1}{a\sigma-1} \theta_P^{\frac{a\sigma}{a\sigma-1}} \right]^{1/\sigma}$ is an *investment multiplier* capturing that parents’ investments become more effective as their skills increase, but to a degree that depends on whether inputs made at home or in an institutional setting are substitutes or complements.¹⁸ Thus, $H(\theta_P)$ captures the inequality in total investments in a given period for a given time parents spend at home x_t .

Equation (14) furthermore shows how this paper’s framework nests the original technol-

¹⁷Note that function $G(\cdot)$ now for simplicity aggregates time e_t , monetary contributions to neighborhood selection $\kappa w h_1$, and a term of unknown unit \underline{G} , and thus assumes that all feed into institutional quality with equal magnitude (or have been normalized to the same scale). Also, not modeling the production of institutional investments with a “return” of parents’ skills on time spent on school choice e_t amounts to assuming that all parents share a common effectiveness of their time of 1.

¹⁸ $\frac{\partial H}{\partial \theta_P} > 0$ as long as $1 + \frac{a\sigma}{a\sigma-1} \theta_P^{\frac{a\sigma}{a\sigma-1}} > 0$ which it will be in all but a few special cases where θ_P is close to 0 and $a\sigma$ is close to 1.

ogy of skill formation from [Cunha and Heckman \(2007\)](#). As the *outer frame*, the technology can be expressed as a function of initial child endowments, θ_0 , parental investment decisions, x_t and skills θ_P , and between-period elasticity of substitution $\frac{1}{1-\phi}$ with both static and dynamic complementarity of investments. But underlying this, parents optimize conditional on an *inner core* that is both determined by the productivity of the time spent with children at home relative to the time spent out-of-home, and the between and within period marginal utility of consumption and leisure. This inner core extends the previous literature by yielding two main insights:

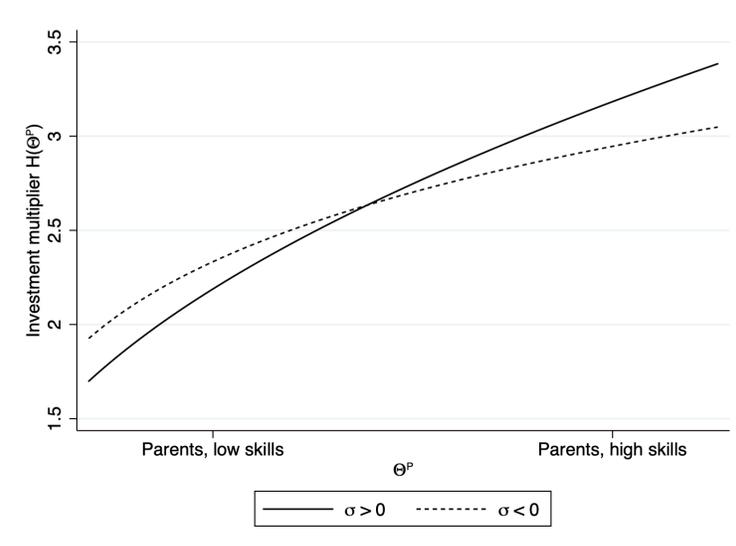
i) Parents spend less time with their children than they would without time constraints where today’s labor and residential choices affect the future possibility of school choices. This finding arises as parents optimize conditional on the marginal utility of consumption relative to the marginal utility of leisure, such that $c_1 = w \frac{\alpha}{1-\alpha} d_w l_1$, and the marginal utility of leisure across periods yields $l_2 = d_w l_1$.¹⁹ The adjustment by d_w reflects the cross-period dependence of neighborhood choice.

ii) How parents distribute time between time at home and time spent on sorting depends on their skills and the elasticity of substitution between investments at home and in institutions.

While insight i) points to the general challenges faced by families with small children, insight ii) has important implications for inequality and the role of public investments. We illustrate this in [Fig. 1](#), which plots the investment multiplier $H(\theta_P)$ for different values of parental skills θ_P and σ . For a given level of parental time investments x_t , greater *substitutability* between home and institutional investments *increases* inequality in total investments between high- and low-skilled parents. The reason is that sorting here becomes a more productive way to influence total investments, which favors those with the best sorting opportunities (i.e. the highest income).

¹⁹The two latter terms are obtained assuming that $u(c_t, l_t) = \alpha \ln(c_t) + (1 - \alpha) \ln(l_t)$.

Figure 1: Parental skills and investment multiplier



Note: The figure shows simulated values of $H(\theta_P) = \theta_P^a \pi^{\frac{1}{\sigma}} \left[1 + \frac{\pi}{(1-\pi)} \frac{1}{a\sigma-1} \theta_P^{\frac{a\sigma}{a\sigma-1}} \right]^{1/\sigma}$ assuming that $a = b$ and $\pi = 0.5$, and $\sigma = -0.7; 0.7$, respectively.

2.4 The Effects of Increasing a Public Input into Institutional Investments

The main equilibrium condition Eq. (5) of the general set-up already tells us how parents may respond to an exogenous increase to public inputs \underline{G} : In optimality, the marginal productivity of home investments should equal the marginal productivity of institutional investments. Increasing institutional quality through higher public inputs \underline{G} will lower the marginal product of the inputs to $g()$, and thereby generate a parental response either through x_t and/or e_t to satisfy the optimality condition again. Parents can thus respond either by *increasing* home investments (i.e. spend more time with their child) or by *reducing* time spent on sorting. In Section 5 we will show that these are exactly the responses we observe in the data following the intervention. How parents respond depends on parents' skills and the whether the two investment types are substitutes or complements. These model predictions of offsetting possible reactions do not depend on any functional form assumptions or borrowing. The long run effect of increasing \underline{G} in period 1 on children's skills equals:

$$\begin{aligned}
\underbrace{\frac{\partial \theta_2}{\partial \underline{G}}}_{\text{Long run effect}} &= \underbrace{\frac{\partial \theta_2}{\partial \theta_1}}_{\text{Self-productivity}} \underbrace{\frac{\partial \theta_1}{\partial \underline{G}}}_{\text{Immediate treatment effect}} + \underbrace{\left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right)}_{\text{Parents' adjustment of inputs}} \underbrace{\frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2}}_{\text{Marginal productivity of parents' adjustments}}
\end{aligned} \tag{15}$$

The effect consists of two overall components. The first is the direct effect on children's skills and subsequent self-productivity from increasing public investments. The second is through parents' responses on home investments and sorting, respectively. Eq. (15) thereby stresses the importance of determining whether home and institutional investments are complements or substitutes. While the first component suggests a positive long-run effect, the sign of the second component is not clear as the sign and magnitude of $\left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right)$ is ambiguous.

In our empirical setting (which we will introduce in Section 3) we consider a RCT in the preschool setting (period 1), which exogenously increases the quality of public institutions (for a given institutional choice in period 1). Hence, from the parents' perspective, the basic quality of institutions \underline{G} appears higher for the treatment group than for the control group, which implies that parents in the treatment and control groups now make their period 2 investment decisions based on different assumptions about the quality of public institutions.

To arrive at more precise predictions from this setting, however, we must focus on the more specific model from Section 2.3 (and setting $a = b$ for simplicity here): The equilibrium condition becomes $x_2 = \frac{\pi}{1-\pi} \theta_P^{\frac{a\sigma}{1-a\sigma}} (\underline{G} + \kappa h_1 w + e_2)$. The term $\theta_P^{\frac{a\sigma}{1-a\sigma}}$ defines whether adjustments to an increase in \underline{G} will be easiest by increasing x_2 on the left-hand side or by decreasing parental input e_2 into institutional quality on the right-hand side.²⁰ If $\sigma > 0$, $\theta_P^{\frac{a\sigma}{1-a\sigma}}$ will be increasing in θ_P , meaning that for high-skilled parents, a small decrease in e_2 goes further in re-establishing balance than increases in x_2 , which would have to be relatively large. In other words, this will make parents with high skills more inclined to reduce the

²⁰This term $\theta_P^{\frac{a\sigma}{1-a\sigma}}$ arises from the definition where quality of time at home x_t varies with parents' skills (and not the specific formulations of $p()$, $g()$ such as separability).

sorting rather than meet higher public investments with more time with children at home. If $\sigma < 0$, the scaling term will be decreasing in θ_P , making high-skilled parents more inclined to adjust their home investments. Thus, how high- and low-skilled parents react to an increase in \underline{G} will reveal whether σ is positive or negative, and thus whether home and institutional investments are complements or substitutes. This framework provides us with a simple test of whether home and institutional investments are substitutes or complements:

- The two investment types are substitutes ($\sigma > 0$) if the RCT shows high-skilled parents reducing their sorting efforts after the RCT (i.e. in period 2: school) more than low-skilled parents, while low-skilled parents adjust their home inputs relatively more.
- The two investment types are complements ($\sigma < 0$) if the RCT shows that high-skilled parents increase home inputs more and sorting effort less than low-skilled parents.

3 The Empirical Setting

3.1 Preschool in Denmark and the Intervention

Childcare (nursery and preschool) in Denmark is heavily subsidized, and municipalities (local-area governments) are obliged to provide childcare slots for all children (Datta Gupta and Simonsen, 2010).²¹ The typical child will start attending nursery at about 12 months old and preschool begins at age 3. Preschool enrollment rates of all 3- to 5-year-old children are near-universal at 97%. Preschool classrooms comprise around 20 children with an adult-child ratio of around 1:7 (Slot et al., 2018). Most preschool staff are trained pedagogues (60%) with a 3.5 year college degree, and the remainder either have completed short courses in pedagogy or are unskilled.²² While Danish childcare-institutions are characterized by a

²¹Redistribution between municipalities ensures that expenses do not vary strongly across areas. There is virtually no private market for preschools in Denmark.

²²Pedagogues' education focuses on children's socio-emotional development. However, to keep a common terminology to other studies in preschool settings, we label preschool staff *teachers*.

high level of expenditures compared to other countries (Esping-Andersen et al., 2012), substantial sorting by parental income and wealth is already apparent when the child is enrolled in nursery (Landersø and Heckman, 2016).

Danish preschools operate from broad “learning schedules” (and not from a single formal curriculum), which focus on comprehensive personal development, social relations, motor skills, outdoor life, culture, values, and relationships (Danish Ministry for Children and Social Affairs, 2018; Slot et al., 2018), but not development of language and (pre-)literacy skills.²³ Slot (2018) finds that Danish preschool-children generally have higher quality interactions with their peers, while interactions with preschool teachers display a lower quality compared with countries such as Germany and the U.S.

Within this setting, a language and literacy intervention took place that randomly improved the quality of teacher interaction with the children in preschool. The intervention **LEAP** (Language Education Activities for Preschoolers; *Fart på sproget* in Danish) provided training of language and (pre-)literacy skills with children aged 3–5 in preschool (parents were not treated, Bleses et al., 2018).

Prior to the intervention, teachers in the treatment group were trained for two days where they also received instructions on how to identify the various learning objectives, and discussed how the specific content could be implemented. During the intervention, the curriculum was kept open such that the intervention provided teachers with teaching material, examples, and professional supervision and instruction, but ultimately allowed each teacher to retain autonomy on how the lessons should be organized and rolled out. Thus, teachers also had autonomy to vary the focus of specific learning objectives. Preschool teachers in the control group participated in a one-day workshop on topics relevant to the daily routines in a preschool. Furthermore, the intervention involved an initial introduction

²³In Denmark, childcare (nurseries and preschools) is placed under the Ministry of Social Affairs (and not the Ministry of Education) as childcare was originally introduced in Denmark as a social policy for low-income and working-class families and not as an introduction to schooling. Therefore, there is no distinction between the learning principles in nurseries and preschools (as opposed to the learning principles in preschools and primary schools, which differ strongly) and the main philosophy in preschools is social-pedagogic and not scholastic (Dahl et al., 2015).

letter to parents (both treatment and control), but other than that parents were not informed about the activities or intervention.

The intervention’s main components were a 20-week period where teachers incorporated play-based activities, sequence and scope, and scaffolding (targeting specific learning objectives as outlined in [Justice et al., 2015](#); [Justice and McGinty, 2012](#)) in the everyday preschool experience.²⁴ The intervention formally consisted of 40 half-hour lessons of high quality language training for children. Each lesson was delivered in small groups with around six children and one teacher, with four groups and two teachers per classroom on average in our sample. However, as the intervention was incorporated in the everyday activities, teachers could utilize the intervention’s components throughout the day, and they were encouraged to continue using the components after the formal end of the intervention as well.

More broadly, due to existing practice in Danish preschools, the intervention introduced a component — systematic focus on language and pre-literacy skill development — to the treatment group that is largely absent in the control group. In addition, as the everyday in Danish preschools is focused on play and socialization activities, the intervention did not crowd out other learning activities. [Bleses et al. \(2018\)](#) present the average short run effects (i.e., after around 6 months) of the intervention, which we also reproduce below.²⁵

²⁴The objectives are concentrated in four domains: i) Vocabulary objectives, e.g., *to understand and use words for the names of unfamiliar objects (nouns) and actions (verbs) and that describe things and actions (adjectives and adverbs)*; ii) Narrative objectives, e.g., *to identify and describe the setting and characters of a story*; iii) Print knowledge objectives, e.g., *to recognize that print carries meaning and to distinguish print from pictures*; iv) Phonological awareness objectives, e.g., *to segment words into syllables and to blend syllables into words*.

²⁵The full roll-out of the LEAP project includes several treatment arms as described in [Bleses et al. \(2018\)](#). This paper focuses on the treatment arm LEAP-OPEN, which only varies the quality of teacher’s interaction with the children and not other components of the everyday in preschools (such as introducing scripted lessons), and thereby provides a direct test of the paper’s central research question. There is no overlap between treatment arms in the preschools.

3.2 Primary School in Denmark

In Denmark, compulsory school starts at grade zero (corresponding to Kindergarten in the U.S.) at age 6, and the vast majority of Danish school-age children attend public schools.²⁶ All Danish public schools have a common curriculum and there is no tracking during primary and lower secondary school. Schools are financed by local municipalities, but regulated via a national per pupil expenditure rate that is made possible via a strong progressive redistribution between municipalities. Thus, there is not as strong of a link between local area public finances and school expenditure as in, for example, the U.S. In fact, as Danish schools receive higher rates for special needs children, the schools with the largest budgets are those with the most disadvantaged students. The distribution of expenditures across public schools in Denmark is very compressed while the U.S. counterpart has large tails both above and below the average expenditure level (see Fig. A.2a). Moreover, teacher wages in Denmark are set by collective bargaining and schools cannot attract higher quality teachers by increasing wages. Most teachers earn within $\pm 5\%$ of the median wage (see Fig. A.2b), which corresponds to the roughly 5% variation in bargaining for different regions in Denmark to align purchasing power between rural and urban areas. Moreover, there is virtually no association between teachers' academic skills (proxied by their own high school GPA) and their hourly wages.

Yet, parents and teachers still sort. Access to a specific school is determined via school catchment areas. Thus, the main eligibility criterion is based on home-address. Moreover, most schools will have a few open slots for children from outside the catchment area, and access via this channel is mainly a function of parents' efforts. [Landersø and Heckman \(2016\)](#), of which Fig. A.3 is reproduced, illustrated the sorting in Danish schools, here exemplified by a strong positive association between school peers' family income and the child's own educational outcomes. In schools serving many low income families, high school completion

²⁶In 2017, 83% of children in grade 0 and 1 attended public schools, and private school enrollment in the lowest grade levels is concentrated mainly in schools that cater to religious minorities in Denmark such as Muslims or Catholics.

rates are below 50% and few attend college, whereas in the most affluent areas high school completion rates are close to 100% and almost all attend college. As we will show in Section 4 (e.g., Figs. 2 and A.4) a similar sorting takes place on the teacher side. Thus, while school expenditures are heavily regulated in Denmark, there is still strong variation in school quality in terms of both the body of students and teachers, generating a Matthew-effect where children from the most affluent families attend schools with higher-quality teachers.

4 Data

We construct a novel data set that combines the following three components (the data construction is detailed in Appendix C).

Intervention Data The intervention provides the exogenous shock to the quality of public investments. The intervention included preschools from eight municipalities located in different parts of Denmark,²⁷ constituting more than 1% of all preschoolers in Denmark during that year. In total, 2,300 children from 73 preschools were part of the study — 1,150 children in the treatment group (36 institutions) and 1,150 children in the control group (37 institutions), respectively. Randomization was at the institution level and stratified within municipalities. Since the intervention focused on language skills for native-speakers, our sample excludes immigrants.²⁸

Before and after the intervention, language tests were collected, mostly by the staff in the preschools. We label these pre-trial and post-trial test scores, respectively. The language tests follow the official language screening used in Danish preschools (Bleses et al., 2018).

²⁷Aabenraa, Faxe, Gentofte, Halsnaes, Copenhagen, Lejre, Rudersdal, and Skive.

²⁸Not all children have aged into grade 2 (and a few children from our sample attend private schools that do not use the grade 2 tests), and not all parents responded to our survey. Our sample with test scores and survey responses include 1,560 and 1,397 children, respectively. We do not restrict the sample to observations without missing outcomes when we present results in the main text. Table A.1 shows that the initial treatment effects and subsequent fade-out remains after dropping observations with missing variables.

Follow-up Survey Around 3 years after the intervention, we conducted a follow-up survey of the parents.²⁹ The invitation to participate in the follow-up survey was sent via secure email to both treatment and control groups. Parents who did not complete the survey within 10 days were subsequently contacted via telephone. We obtained a response rate of 60%. There are no significant differences in survey response by treatment status.

In the questionnaire, we asked parents about activities relating to support of their children’s language development. We construct a measure for parental direct time investments in their children with confirmatory factor analysis including items such as “I enjoy reading for my child.”, “I am often too busy or too tired to read to my child.”, and “How many times last week has your child been read to (or read with) at home?” (see Section C.4 for the full list of questions and factor loadings).

Register data We link each child and its parents to full population register data using the unique individual identifier of the child’s social security number. The registers provide rich information, which we utilize to obtain a unique data set on not only the intervention but also the children’s family and local environment.

i) Child skills: We obtain a longer-run measure of child skills from compulsory test scores in grade 2 (age 8–9) testing children’s reading, language and literacy skills.³⁰

ii) Parent characteristics: The register data also include unique links to parents’ individual identifiers allowing us to link each child to their family, home address, and parents’ income, employment status, and education. Moreover, having access to full population register data, we are not only able to characterize each child’s family, we also observe the environment they grow up in and which schools they attend. We proxy parental skills by their education, where we categorize them by their highest recorded years of schooling, clas-

²⁹See Section C.1 for more information and the detailed set of questions.

³⁰The tests take place near the end of the school year and are computerized adaptive tests in which questions are determined by the student’s performance earlier in the test. The tests are scored electronically without teacher input. They measure three underlying constructs: Reading comprehension, decoding, and language comprehension. Following Sievertsen et al. (2016) and Beuchert and Nandrup (2018), we standardize these three individual scores, take the simple average, and re-standardize them within year.

sifying parents where none has at least 14 years of schooling as “Less than college” (35% of our sample), and those where at least one has 14 or more years as “College or higher”.

iii) School quality: We define this as a measure of how the average characteristics of teachers working at a given school predict that the children at the school do well in compulsory (externally scored) tests. We base this on a unique dataset linking all teachers in Denmark and the schools at which they work at from 2010 to 2016. From the unique individual identifier, we merge teachers’ identifiers to information on age, tenure, year of graduation, high school GPA, high school GPA in language subjects, teacher college GPA, and unemployment spells, and calculate the school averages. We link each school with the individual standardized (and externally scored) language test scores for all children from grades 2 through 8 during the years in question, and regress children’s test scores on the average teacher characteristics in the school they attend. We rank the predictions from this regression from 0 to 1, with 0 being the school where the teachers with the least favorable observable characteristics work and 1 the school where the teachers with the most favorable observable characteristics work.³¹ We focus on overall school quality and not, for example, specific teacher value added because parents’ enrollment decisions are made when they only have information about the school’s average characteristics and not what specific teachers their child will be exposed to.

Fig. 2a presents average test scores across the estimated school quality for all public schools in Denmark. The figure shows that average test scores in schools increase by roughly one standard deviation from the “worst” to the “best” schools as defined by teachers’ observable characteristics. Next, Fig. 2b plots parents’ average years of schooling against estimated school quality. There is a strong association between parents’ education and teacher characteristics in schools. On average, parents with children in the “worst” schools hold almost 2

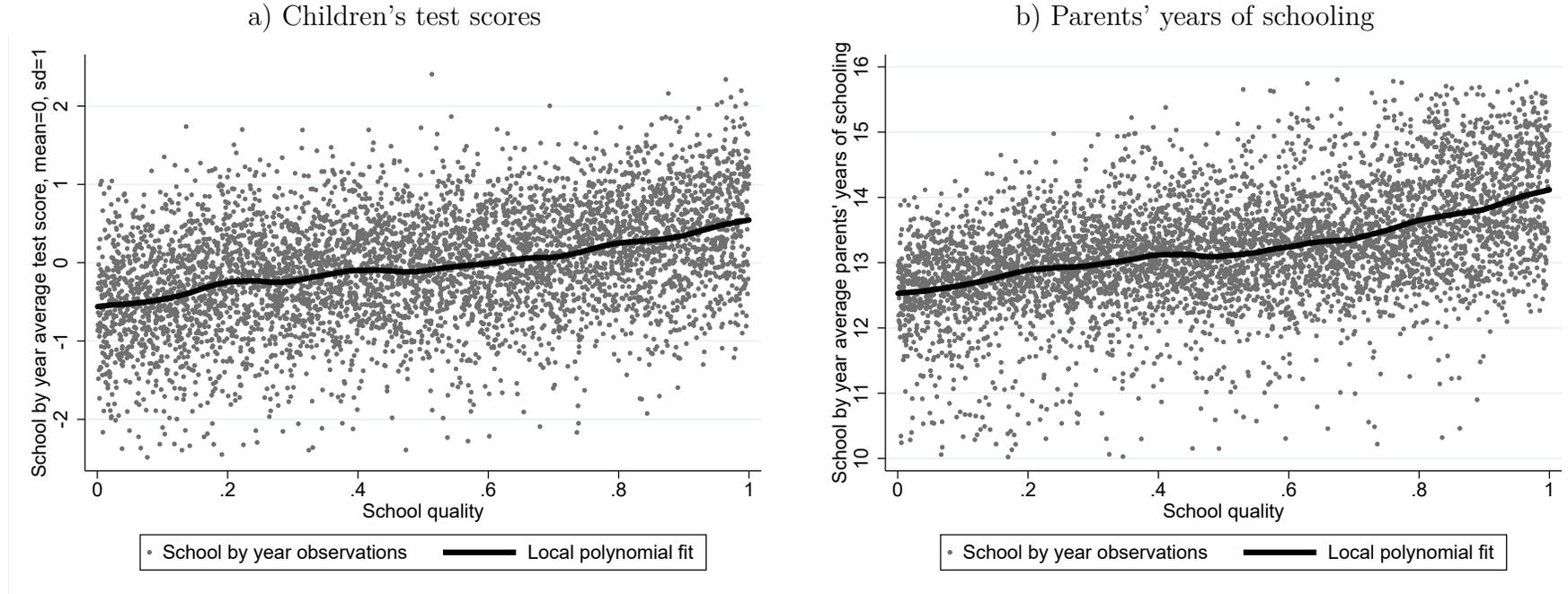
³¹School quality is estimated based on 94,770 individual teachers (around 50,000 teachers each year from 2010 to 2016) linked to 5,557 schools by annual observations for a total of 1,526,234 observations of children’s standardized test scores.

years less education than parents with children in the “best” schools.³²

Table 1 presents an overview of when the main variables of our analysis were measured, and what model components they relate to. The pre-trial test scores were collected a few weeks before the intervention, and the post-trial test scores shortly after. Then, in 2016, 3 years after the intervention, the parent survey was collected and in 2017 or 2018 we measure children’s language test scores and rank the schools they attend by teacher characteristics.

³²Table A.2 shows by school quality decile the 10th percentile, median, and 90th percentile of the standardized test scores. Within each decile of school quality, the 10th and 90th percentiles of average test scores differ by approximately 1.7 standard deviations. Fig. A.4 shows the association between our measure of school quality and average property value of the homes of the students in a given school. Also, note that the estimated school quality is also strongly correlated with parents’ statements of satisfaction with their child’s school from the survey (see Fig. A.5).

Figure 2: Children's standardized test scores and parents' years of schooling, by estimated school quality



Note: The figure shows a) school by year average test scores (for children from grade 2 through 8) and b) their parents' years of schooling plotted against the estimated school quality measure from teachers' observable characteristics. Test scores are standardized to mean 0 and standard deviation 1 at year and grade level. The figure also shows a local polynomial smoothing of the relationship between average test scores / parents' years of schooling and estimated school quality. The figure is based on data for all children and public schools in 2010-2016.

Table 1: Timeline of outcome measurements

Timing	Age	Event	Data
-3 – -6 months	3–5	Baseline data collection	Language test scores θ_0
0 – +5 months	3–6	<i>Intervention</i>	Changing \underline{G}_1
+10 months	4–7	Endline data collection	Language test scores θ_1
+3 years	6–8	Parent survey	Parents’ investments x_2
+4 – 5 years	7–9	In school tests	Language test scores θ_2
+4 – 5 years	7–9	Register data	School characteristics / quality $\underline{G} + \kappa h_1 w + e_2$

Note: Timing is relative to the intervention.

4.1 Descriptive Statistics and Balancing

Table 2 presents in column 1 the background characteristics of all children in Denmark born during the same years as our main sample. Columns 2 and 3 present the background characteristics for our control and treatment groups, and column 4 presents the mean differences between the treatment and control groups. The table shows that the mean characteristics of children in our sample correspond to the average characteristics of children in those cohorts, with the exceptions that parents in our sample are marginally older, have 0.2 years more schooling, and the mothers have higher employment rates compared to the average parent in the overall population.

Importantly, Table 2 also shows that of the 19 covariates only two are significantly different at the 10% level when we compare the treatment and control group. In a joint test where treatment status is regressed on all the covariates, three of the 54 tests are significant at a 5% level and two at a 10% level (Table A.3). The results from the balancing tests correspond to what could be expected from random variation. As a further test, Fig. A.6 shows that there is virtually no variation in predicted outcomes from covariates across treatment status: While the actual post-trial test score distributions differ strongly between the treatment and control group, differences in the distributions based on the predictions from covariates are barely detectable.

Fig. 3 presents distributions of the key variables by parents’ education for the control

Table 2: Balancing of estimation sample by treatment

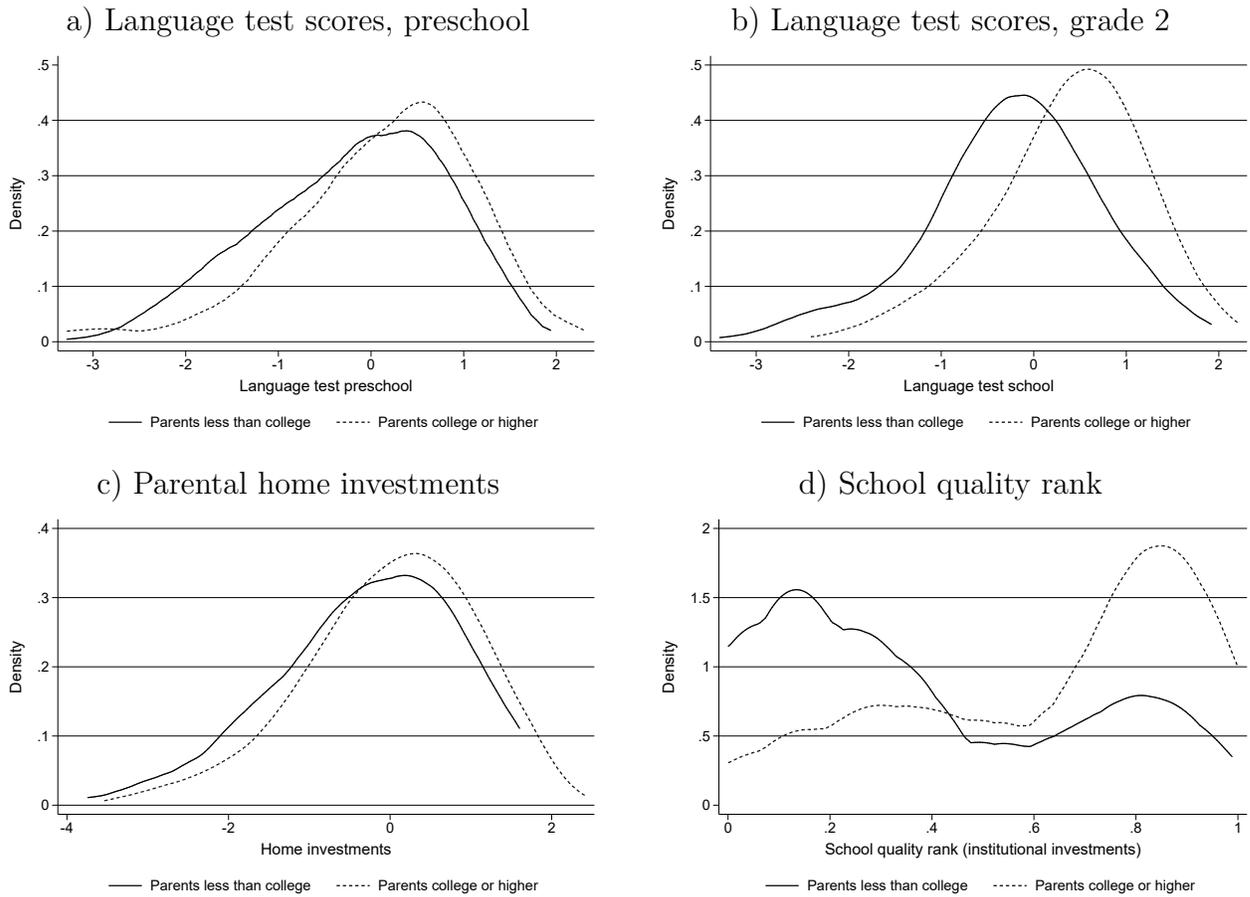
	(1) General Pop	(2) Control Avg.	(3) Treated Avg.	(4) Diff Treat-Control
Pre-trial Test		-0.037 (0.994)	0.039 (1.013)	0.076 (0.087)
Child's age at pretest	4.044 (0.840)	4.086 (0.849)	4.041 (0.851)	-0.045 (0.044)
Born in 2007	0.253 (0.434)	0.191 (0.393)	0.174 (0.379)	-0.017 (0.046)
Born in 2008	0.256 (0.436)	0.330 (0.471)	0.330 (0.470)	-0.001 (0.023)
Born in 2009	0.246 (0.430)	0.295 (0.456)	0.331 (0.471)	0.037 ⁺ (0.022)
Born in 2010	0.246 (0.431)	0.177 (0.382)	0.157 (0.364)	-0.021 (0.043)
Male	0.514 (0.500)	0.537 (0.499)	0.504 (0.500)	-0.032 (0.026)
Child's birth weight, kg	3.478 (0.604)	3.517 (0.482)	3.464 (0.520)	-0.053* (0.024)
Gestation length, weeks	39.627 (1.945)	39.775 (1.555)	39.698 (1.593)	-0.078 (0.080)
Apgar score	9.863 (0.620)	9.852 (0.591)	9.876 (0.594)	0.023 (0.029)
Number of siblings	1.382 (0.851)	1.390 (0.860)	1.323 (0.786)	-0.067 (0.058)
Mother's weight, kg	67.569 (38.923)	66.498 (16.691)	67.471 (15.626)	0.973 (1.258)
Mother years of schooling	13.934 (2.457)	14.180 (2.510)	14.113 (2.435)	-0.067 (0.305)
Mother's age, 1/9-17	39.153 (5.050)	39.876 (5.111)	39.821 (4.973)	-0.054 (0.555)
Mother employed in 2012	0.788 (0.409)	0.830 (0.376)	0.845 (0.362)	0.016 (0.025)
Father years of schooling	13.678 (2.438)	13.949 (2.419)	13.863 (2.422)	-0.086 (0.296)
Father's age, 1/9-17	41.531 (5.777)	42.395 (6.020)	41.997 (5.637)	-0.398 (0.525)
Father employed in 2012	0.872 (0.334)	0.889 (0.315)	0.886 (0.318)	-0.003 (0.022)
Household wage income 2017, \$1,000	89.241 (58.087)	100.056 (72.152)	99.375 (61.301)	-0.681 (8.310)
N	2,744	1,150	1,150	2,300

Note: The table shows descriptive statistics for all children in Denmark in the same birth cohorts as the paper's sample (column 1), the control group (column 2), and the treatment group (column 3). Average treatment-control differences are shown in column 4. Standard deviations of the variables are shown in parentheses for columns 1-3, standard errors clustered at institution level for column 4. The general population (column 1) consists of all children born in 2007-2010.

*($p < 0.10$), **($p < 0.05$), ***($p < 0.01$).

group. There are substantial differences between language skills in preschool (Fig. 3a), and they grow as the children reach primary school (Fig. 3b). The distribution of the parental investment factor also differs across parents' education (Fig. 3c). Similarly, the school quality rank of the children's schools is also strongly associated with their parents' education level (Fig. 3d).

Figure 3: Children's test scores and parents' investment measures in the control group, by parents' education



Note: The figure shows distributions of the key measures; children's language test in preschool (after treatment) and school (a and b) in standard deviations from the mean, the parental home investment factor (c) in standard deviations from the mean, and school quality rank (d), by highest education of parents. If the highest of the two parents' years of education is below 14 years, they are classified as "Parents less than college", vs "College or higher." The figure is based on data for the control group.

5 Results

5.1 Main Effects on Test Scores

Figure 4 shows the distributions of language test scores measured before the intervention, shortly after the intervention, and in grade 2, by treatment status and by parental education. There are no treatment-control differences in the pre-trial language test scores, but clear differences in test scores measured shortly after the intervention. By grade 2, however, any treatment-control differences for children whose parents have a college degree have vanished.

Fig. 5 presents the estimated average treatment-control differences in language test scores. These are estimates of β in the regression:

$$y_{it} = \alpha + \beta_i T_i + \varepsilon_{it}$$

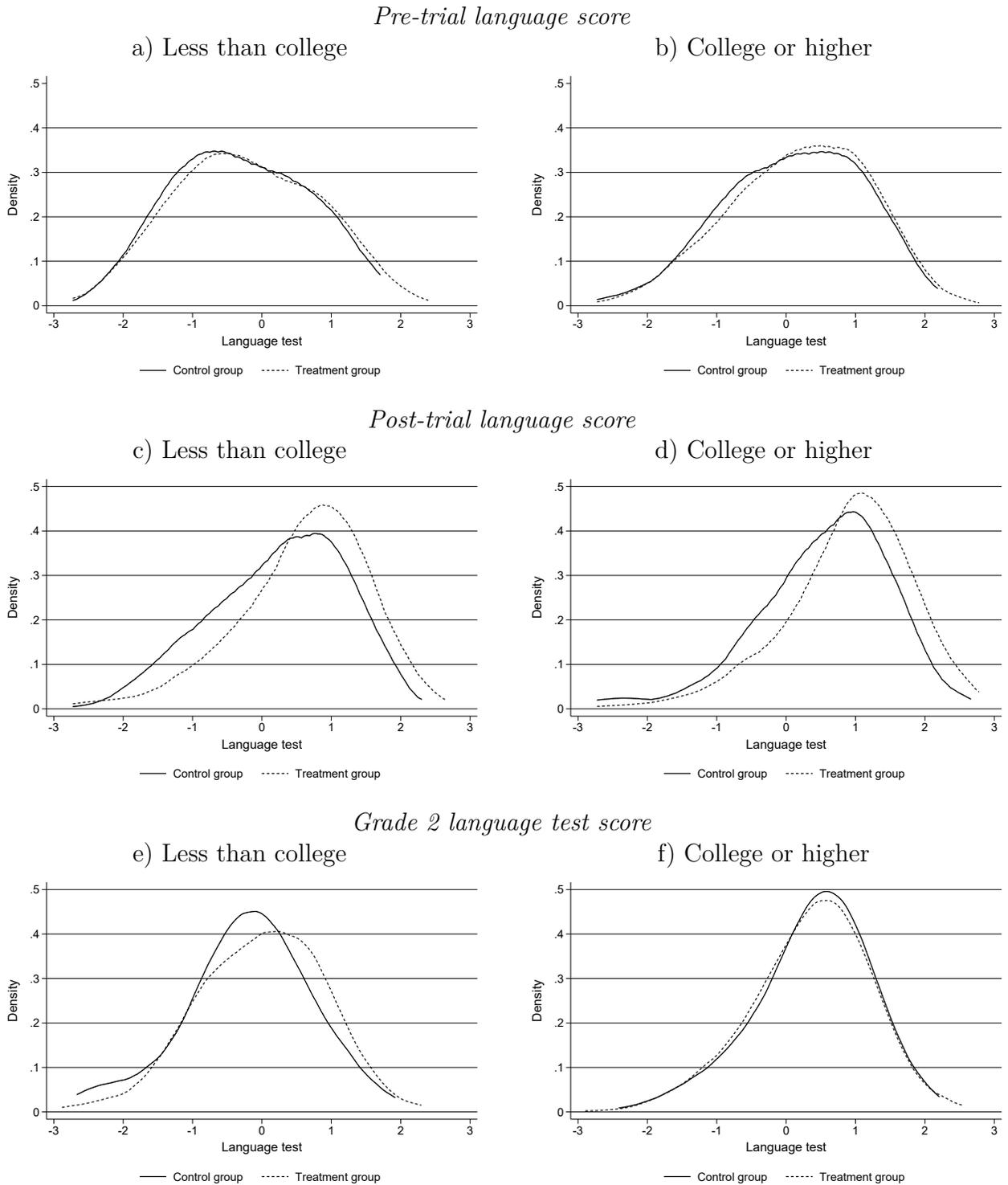
where y are language scores at the different time points t and T is the treatment indicator.³³ The left panel of Fig. 5 shows a small and insignificant difference in mean test scores prior to the intervention, followed by a large treatment effect of roughly 0.35 of a standard deviation in the language test score shortly after the trial (which reproduces the findings from [Bleses et al., 2018](#)). This initial treatment effect is remarkable and the intervention, thus, provides an ideal setting for studying parents' responses and longer-run effect on children's skills when preschool quality changes.

As a natural next step, the final bar in the figure presents treatment-control differences in grade 2 test scores. While the large average treatment effect appear to have faded, there may be heterogeneity by parental education.

In the two right panels of Fig. 5, we therefore consider the effects separately by parents' highest completed education. While the short run average treatment effects are similar be-

³³The standard errors are clustered at the preschool level. We also repeat this regression in Fig. A.7 with additional controls (namely, all covariates in Table 2). The results remain qualitatively the same, unsurprisingly given the balancing tests presented in Section 4.1.

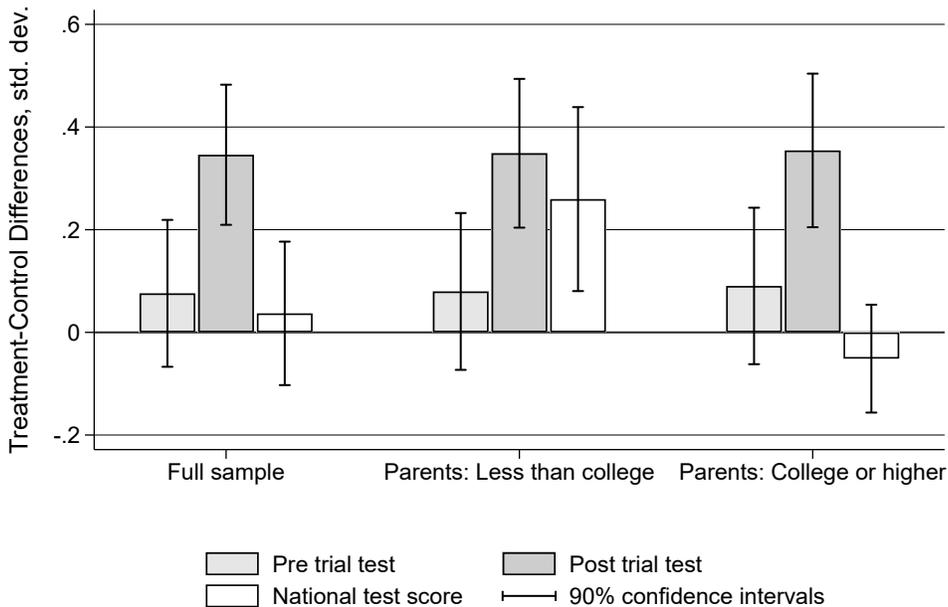
Figure 4: Test score distributions, by treatment status and parental education



Note: The figure shows pre-trial, post-trial and 2nd grade test score distributions for the control and treatment group by parents' education, in standard deviations from the mean. Parents where neither of them has at least 14 years of schooling are classified as "Less than college" vs "College or higher."

tween more and less educated parents (post-trial test), by grade 2 the effects have faded completely for children with parents with at least a college degree, while they remain sizeable at around 0.26 of a standard deviation for children with less educated parents, which corresponds to almost 40% of the baseline test score gap across parental education.³⁴ The long-run treatment effects are significantly different between the parental education groups. This heterogeneity represents a push towards more intergenerational mobility: In grade 2, the association between parental years of schooling and child language scores is much stronger in the control than in the treatment group (see Fig. A.8).³⁵

Figure 5: Baseline balancing, short-run, and longer-run treatment effects



Note: The figure plots estimates of the treatment–control differences (β_t) in test scores y_{it} from $y_{it} = \alpha + \beta_t T_i + \varepsilon_{it}$ with 90% CIs on the treatment indicator. Table A.4 presents the regression output.

However, as parents’ education and children’s pre-trial test scores are highly correlated, it could be that the heterogeneous effects in grade 2 reflect heterogeneity by initial child skill level. This is not the case. When we split the treatment effects on grade 2 test scores by the

³⁴The heterogeneity in treatment effects on grade 2 test scores by parental education is present for each of the three sub-dimension tested: language comprehension, decoding, and text comprehension (Fig. A.9)

³⁵Intergenerational dependence between child and parent skills can be expressed as: $\frac{\partial \theta_2}{\partial \theta_P} = \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial \theta_P} + \frac{\partial \theta_2}{\partial I_2} \left(\frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial \theta_P} + \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial \theta_P} \right)$, which stresses that heterogeneous changes to parental investment decisions both in terms of home and institutional investments also affect intergenerational mobility.

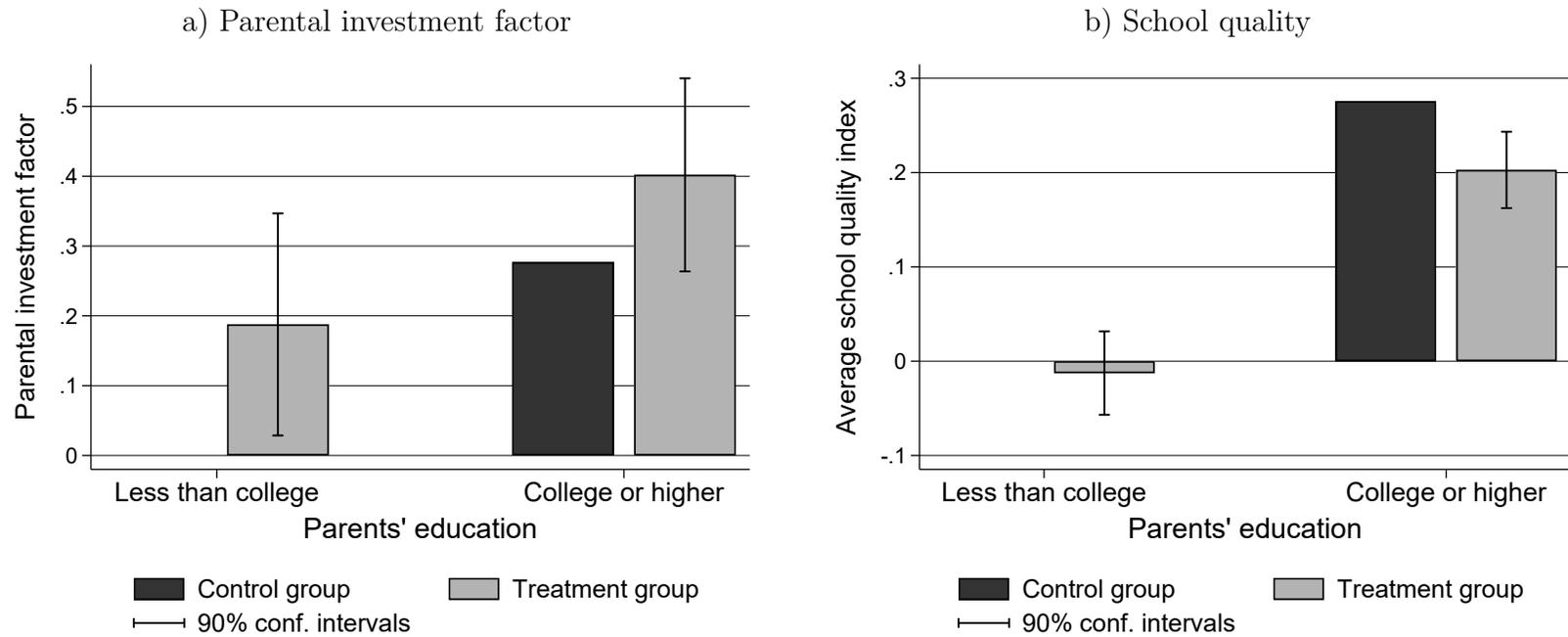
child’s pre-trial test scores, they are uniformly low (see Table A.5). Therefore, we interpret the heterogeneous treatment effects as outcomes of differences in parents’ education (skills).

5.2 Parents’ Responses

What explains the disconnect between the almost uniform treatment effects initially and later heterogeneity across parental education? As a first step, Fig. 6a shows the treatment–control differences in the parental home investment by parents’ education normalized relative to the lowest education category in the control group. The black bar shows a substantial difference in parental home investments in the control group where the investment factor is almost 0.3 of a standard deviation higher among college educated parents compared to parents with less than college. The figure also documents an increase in parental investments following the intervention when comparing the treatment and control groups. The average treatment–control difference is around 0.2 of a standard deviation for parents with high school or less as highest education, but it is only half of that for parents with a college degree or higher (and only borderline significant at the 10% level). This provides the first suggestive evidence of whether parental and institutional investments are substitutes or complements, as low-skilled parents appear to adjust their inputs at home slightly more than high-skilled parents (although this difference is not statistically significant).

Fig. 6b broadens the previous finding for parental investments by considering the quality of the school that children now attend. The figure shows the average rank of school quality by treatment and control group and parents’ education levels. Children of highly educated parents in the treatment group attend significantly *worse* schools. In contrast, there is no change to the schools children with low educated parents attend, which implies a strong (statistically significant) heterogeneous response across parental education.

Figure 6: Treatment–control differences in investments



Note: Fig. 6a shows average of parents' investment factor by treatment status and parental education, with children in the control group with low educated parents as reference category. Fig. 6b shows average estimated school quality by treatment status and parental education, with reference category children in the control group and low educated parents. The 90% confidence intervals test the treatment–control differences; i.e. the difference between each pair of black and grey bars. Table A.6 presents the regression output.

We next assess how parents (children) select into different schools. The left half of Fig. 7a shows, by treatment status, the share of families who move to a new address between preschool and grade 2, and whether movements happen between municipalities (longer distance) or within municipalities (relatively short distance). There are no differences between moving patterns across treatments status. The right half of Fig. 7a shows the proportion of children who stay in the school that most children in the preschool attend (i.e. the modal school the preschool is a feeder for), for those who do not move to a new address between preschool and grade 2, those who move within the municipality, and those who move to another municipality. Children in the treatment group who either do not move or move to a new address within the same municipality (i.e. they move a relatively short distance) are much more likely to attend school with their preschool peers. In other words, parents in the treatment group become less selective in their school choice. As a placebo test, the figure also considers school choices for the children who have moved to another municipality. These are children who, in general, will be unable to attend the school for which their preschool is a feeder irrespective of treatment status. Here, we — reassuringly — find no treatment–control differences (and that very few stay in the modal school).

Fig. 7b confirms this finding. The figure presents the average school quality by moving patterns between preschool and grade 2, and treatment status. The figure first shows that there are no significant control–treatment differences in children’s school quality for children with low educated parents irrespective of their moving patterns between preschool and grade 2. However, turning to children with highly educated parents’, the right part of Fig. 7b shows that the treatment–control differences in school quality are driven by those who either do not move or move a short distance within the same municipality. Thus, the school quality differences are driven by the group that becomes more likely to use the default school where they live.

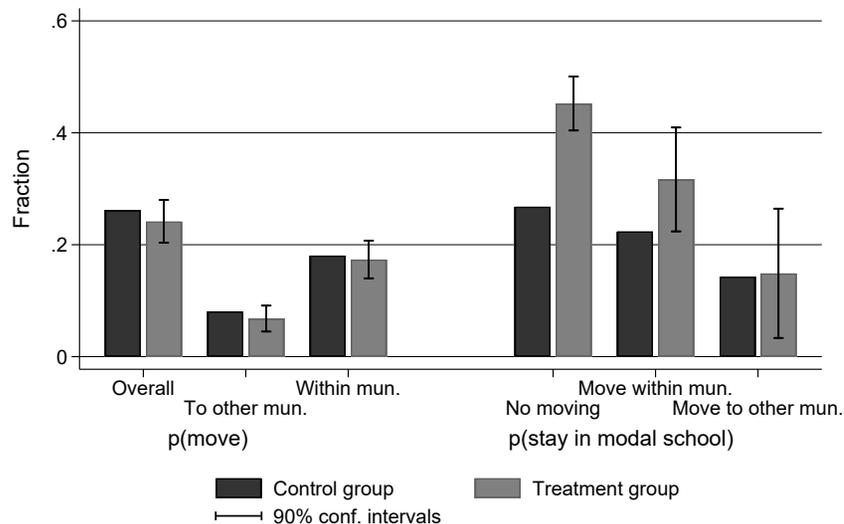
Figs. 6 and 7 thus follow the predictions from Section 2 that parents should increase home inputs and reduce sorting effort. Moreover, reduced segregation by background char-

acteristics during school appears to be a by-product of the increased public investments during preschool. This reduced effort invested in sorting by highly educated parents may be surprising, but two facts help us reconcile this finding. First, note that children of highly educated parents still attend better-quality schools after the treatment. They just do so to a smaller degree in the treatment group compared to the control group. Second, we find suggestive evidence that highly educated parents use some of the time freed up from the reduced sorting effort by increasing their labor supply.³⁶ Our survey contains a rough measure of average hours worked during a day that we use for a simple analysis in Table A.6. While the treatment effects are not statistically significantly different from zero, the point estimates are negative for less-educated parents and positive for highly educated parents. Thus, less educated parents who already work fewer hours per day than high-educated parents to begin with, appear to reduce their average hours worked during the day slightly, while highly educated parents do the opposite.

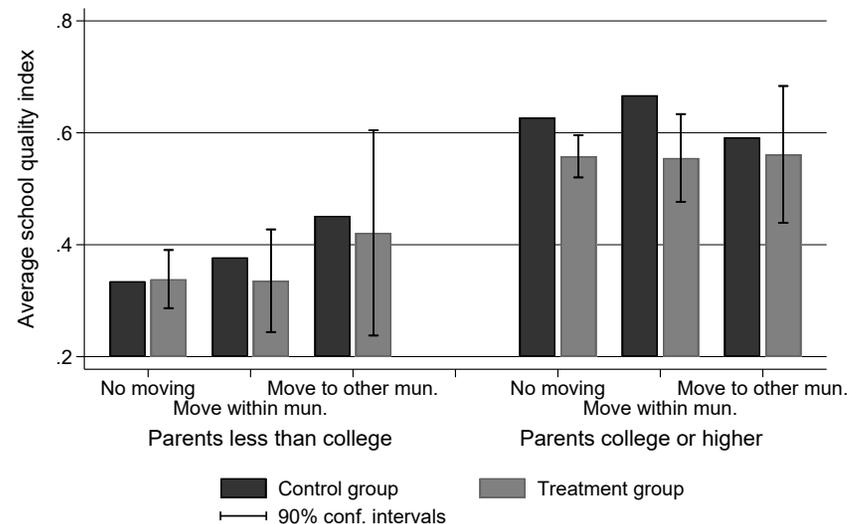
³⁶It should be noted that many parents may not have full discretion over hours spent on work in practice (as opposed to e.g., parents' home investments in their children).

Figure 7: Mobility from preschool to grade 2, school choice, and school quality, by treatment status

a) Mobility from preschool to grade 2 and school choice



b) Mobility from preschool to grade 2 and school quality



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Note: Fig. 7a shows residential mobility (left half of Fig. 7a) and school choice (right half of Fig. 7a) by treatment status. The left half of Fig. 7a shows the fraction of the sample who live at a different address when they attend school relative to when they attended preschool. It shows the overall fraction who move, and whether this is a move within the municipality (i.e. a relatively short distance) or to another municipality. A move within the municipality does not necessarily lead to a change in public institutions. A move to a new municipality in general does. The right half of Fig. 7a shows the fraction of children who attend the modal school (defined as the primary school to which their preschool is primarily linked), for those who do not move between preschool and school age, those who move within the municipality, and those who move to another municipality. Figure Fig. 7b shows average school quality by mobility between preschool and grade 2 (for those who do not move between preschool and school age, those who move within the municipality, and those who move to another municipality) and parents' education (less than college and college or higher). The 90% confidence intervals test the treatment-control differences; i.e. the difference between each pair of black and grey bars.

5.3 Progressiveness of public investments and treatment heterogeneity

In sum, our empirical results show that while the intervention had large initial positive effects on language skills across all backgrounds, the longer-run effects are mediated by parental responses. The intervention in this sense is progressive from the children’s perspective: children with low-skilled parents benefit more than children with high-skilled parents. However, this appears to be a result of differences in parents’ responses.

These findings beg the question of whether the intervention increasing public investments \underline{G} in period 1 was progressive or regressive from the parents’ perspective. We therefore consider how the intervention affects parents’ utility in the final period (as given in Eq. (4) without imposing functional form assumptions to the production functions):³⁷

$$\underbrace{\frac{\partial U}{\partial \underline{G}}}_{\text{Effect of intervention on parents' utility}} = \underbrace{\beta \frac{1}{\theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial \underline{G}}}_{\text{Utility gain from intervention's effect on skills}} + \underbrace{\left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right)}_{\text{Parents' adjustment of inputs}} \left[\underbrace{\beta \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2}}_{\text{Marginal productivity of parents' adjustments}} - \underbrace{(1 - \alpha) \frac{1}{l_2}}_{\text{Marginal utility of leisure from adjustments}} \right] \quad (16)$$

Eq. (16) shows that parents’ utility is affected through several sources: i) the direct effect that a change in public investments has on children’s skills and thus parental utility, all else equal, ii) the change to parents’ inputs in children’s skill formation, iii) the productivity of this change in inputs, and iv) how the changing inputs affect parents’ leisure.

For the intervention to be progressive it must increase the utility of low-skilled parents more than of high-skilled parents: $\partial U / \partial \underline{G}$ should be decreasing in parental skills θ_P . The first term of Eq. (16) is likely decreasing in parents’ skills, as $1/\theta_2$ is highest for children with low-skilled parents. The sum in the brackets is also decreasing in parents’ skills assuming that production functions are concave and because low-skilled parents have higher levels of leisure. However, as we also showed when we discussed whether the intervention reduced

³⁷Derivations in Section B.5.

skills gaps for children, progressiveness from parents' perspective is not ensured if home and institutional investments are complements. In that case, the term $\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}}$ would be increasing in parents' skills. In other words, only if home and institutional investments are substitutes is it certain that the intervention will be progressive.

Public investments are often combined with progressive taxation as funding. The key relationship in this paper arises as a result of parents' responses and the opportunity costs of their time, which determines who benefit from the intervention. A natural next question is then whether a progressive tax $\tau(\theta_P)$ on parents' income would ensure that the intervention is progressive irrespective of whether home and institutional investments are complements or substitutes.

An income tax will not affect the essence of parents' trade-off: whether to devote time to influence home or institutional investments. The term $\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}}$ remains as a determinant of whether the intervention is progressive or regressive from the parents' perspective irrespective of taxation: whether to use one hour to invest in children is determined by the opportunity costs of time and thereby by an income tax, but how this additional hour is spent depends on the relative productivity of home and institutional investments.³⁸

Thus, the elasticity of substitution between home and institutional investments results in a complex set of trade-offs. On the one hand, we showed earlier that the *investment multiplier* in the baseline would favor children with high-skilled parents most if home and institutional investments are substitutes (as high-skilled parents could then focus on labor supply and invest in children through institutional sorting). On the other hand, increasing public investments would not necessarily be progressive from children's and their parents' perspective unless home and institutional investments are substitutes (as this makes sorting less influential as an input in skill formation).

³⁸In our specific case we obtain $\frac{\partial U(c_2)}{\partial l_2} w(1-\tau) = \frac{\partial U(l_2)}{\partial l_2}$ from the additive separability and $\frac{\alpha}{1-\alpha} w(1-\tau) l_2 = c_2$ from the log-specification in the utility function, which cancels out. More generally, however, τ will only change the relative price of consumption/leisure, and not whether parents should devote time of x or e .

5.4 Implication of Heterogeneous Treatment Effects for the Substitution Parameter

What can we say about the elasticity of substitution between home and institutional investments from the intervention? The treatment effects persist for children from low-skilled parents because the improved preschool quality improved their own skills (skills beget skills) and because parents increased their inputs after observing the higher quality of institutions. The treatment effects for children with high-skilled parents, however, fade as parents become less selective in their school choices. This finding (assuming that the production functions have CES structure) is compatible only with parental and institutional investments being *substitutes* (i.e. $\sigma > 0$).

The more general model without functional form assumptions does not allow us to draw conclusions about the elasticity of substitution, apart from it being a function of parents' joint response on home inputs and institutional sorting when public investments change. The general model can, however, bridge the gap in previous studies, which have found seemingly conflicting results on the question of substitution versus complementarity. [Gelber and Isen \(2013\)](#) find that randomization into the higher-quality Head Start *increases* parental involvement. However, parents can also affect institutional quality. [Fredriksson et al. \(2016\)](#) study students in grades 4 through 6 and conclude that lower quality of public schools leads parents to change schools — a conclusion similar to [Pop-Eleches and Urquiola \(2013\)](#), who find that parents lower investments in response to better high school quality. But as our model illustrates, it is not sufficient to observe whether parents increase or decrease one type of input.

Moreover, the complete fade-out for children with high-skilled parents is remarkable and comparable to [Currie and Thomas 2000](#), who also find full crowd-out as they use school sorting as a margin of adjustment. This finding raises the natural question of whether the treatment effect fade-out can be explained by these differences in school choice (or expressed

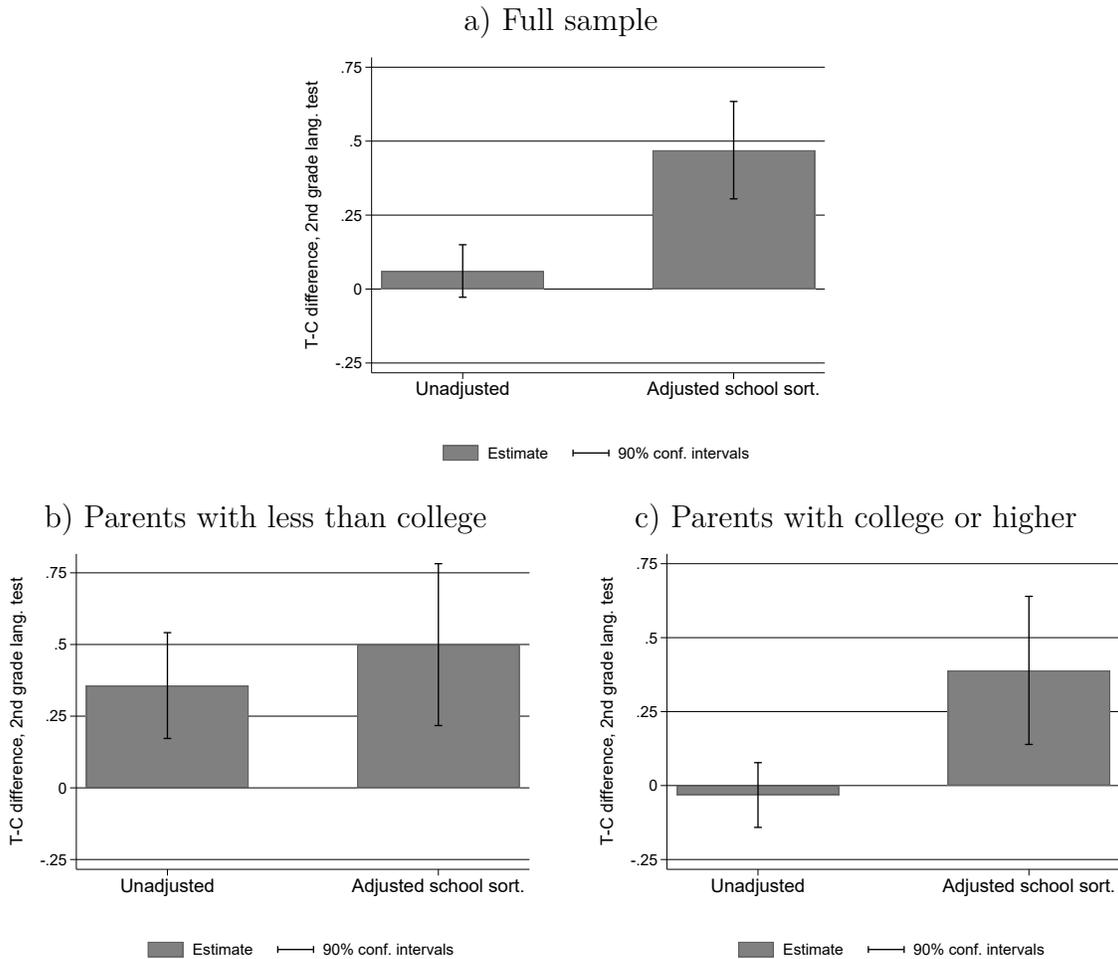
in terms of the model what the treatment effects would be if $\frac{\partial e_2}{\partial \underline{G}} = 0$). We may obtain a proxy of the intervention’s effects on language test scores, *net of any school selection*, by conditioning on school quality in a regression of language test scores on the treatment. Formally, we estimate the following equations

$$y_i = \alpha + \beta T_i + \varepsilon_i \tag{17}$$

$$y_i = \tilde{\alpha} + \tilde{\beta} T_i + \gamma_1 * SQ_i + \gamma_2 * SQ_i * T_i + \tilde{\varepsilon}_i \tag{18}$$

where y_i captures child i’s test scores, T_i denotes their treatment assignment and SQ_i their school quality rank. β corresponds to the treatment–control differences presented in Fig. 5 and $\tilde{\beta}$ to the treatment–control differences net of the changed school selection (at $SQ_i = 0$). As this conditions on an outcome variable (school quality), the estimates should be interpreted with caution. Fig. 8 presents the results, first for all children (a) and then by parental education (b-c). Once we control for school quality, there are large and significant treatment-control differences for grade 2 test scores in the same order of magnitude as found for the short run post-trial tests. Breaking this down by parents’ education, we see that the estimate changes slightly for children with low educated parents (as there is a small change in school choice here), whereas they change substantially for children with higher educated parents. Fig. A.10 extends this finding and shows that it is mainly the middle and lower part of the test score distribution in the treatment group that is shifted, once we control for school selection.

Figure 8: Long-term treatment effects, controlling for school sorting, by parents' education



Note: The figure plots estimates of Eq. (17) by parents' education. The baseline treatment–control differences presented in the bars “unadjusted” present estimates of β , while the treatment-control differences net of the changed school selection $\tilde{\beta}$ are presented in the bars labeled “adjusted for school sorting.” The estimates should be interpreted with caution, as we condition on an outcome variable (school quality) which may bias estimates. However, if unobservables guiding school choice and affecting child test scores are positively correlated, we will underestimate $\tilde{\beta}$.

6 Discussion and Conclusion

This paper studies how parental and public investments in children’s skill formation interact. We do so by first formulating a general model of child skill formation, which includes two types of investments; home investments that are given by parents’ time spent with their child, and institutional investments that are affected both by public investments and parental efforts to sort into higher quality institutions.

The model’s principal implications can be stated as follows: the degrees to which public investments increase children’s skills and reduce gaps between children with different background depend on whether inputs at home and inputs in preschools and schools are substitutes or complements. Without any functional forms imposed on production functions, we show that this elasticity of substitution is given by the relative marginal productivities of parents’ time spent either investing at home or influencing institutional quality via sorting, which in turn depend on the specific home and education production functions. We then gradually impose a minimal set of functional form assumptions to finally arrive at a technology of skill formation with predictions, which we can test empirically via a randomized controlled trial in Danish preschools.

The RCT exogenously increased the quality of preschools, and we link the children from this intervention to full population register data with information on later school choice, school quality, and child test scores. Our empirical analysis shows that increasing the quality of universal childcare reduces skill gaps between children from advantaged and disadvantaged backgrounds. The intervention had large initial positive effects on language skills at ages 4 to 5 across all backgrounds. For children with low-skilled parents, test scores remain 0.26 standard deviations higher in the treatment group than in the control group at ages 8 to 9 (4 to 5 years after the intervention). There is, however, a complete fade-out for children with high-skilled parents who use school sorting as a margin of adjustment thereby offsetting the initial treatment effect. Linking these heterogenous responses to our model shows that they

are only compatible with home and institutional investments being substitutes.

While our findings after imposing specific functional forms may apply with a local range of investment choices, they may not apply globally. Our general version of the model shows that it cannot be determined whether the elasticity of substitution is constant or even has the same sign across the full range of home and institutional quality without specific knowledge about the underlying home and educational production functions. Similarly, while the vast majority of children in OECD countries attend preschool and thus face the intensive margin problem relating to the quality of institutions (which we study), the results and elasticity of substitution between home and institutional investments may be different for the extensive margin problem of whether to send a child to preschool. In addition, our empirical setting focuses on children from preschool age onward, but substitution between different types of inputs may be different when it comes to infants and toddlers.

Moreover, several important considerations emerge if home and institutional investments are substitutes (as our results suggest). One implication of our model is that inequality in investments is largest when home and institutional investments are substitutes because sorting as a means to invest in children's skills is most effective here. Indeed we find that Danish public schools — although funds are equalized through a strong redistribution — are still characterized by sorting both at the family and teacher level. The most able teachers work at schools attended by children from affluent backgrounds, while the least able teachers work at schools attended by children from disadvantaged backgrounds. Our findings, however, also suggest that increased public investments can induce high-resource parents to readjust time use and thereby reduce the effort they put into sorting.

The paper thereby distills a trade-off when designing policies: On the one hand, universal public investments come at a cost if they feed into affluent parents' consumption or leisure. But on the other hand, our results also illustrate the potential of providing investments through public institutions during childhood as a lever to reduce skill gaps between children.

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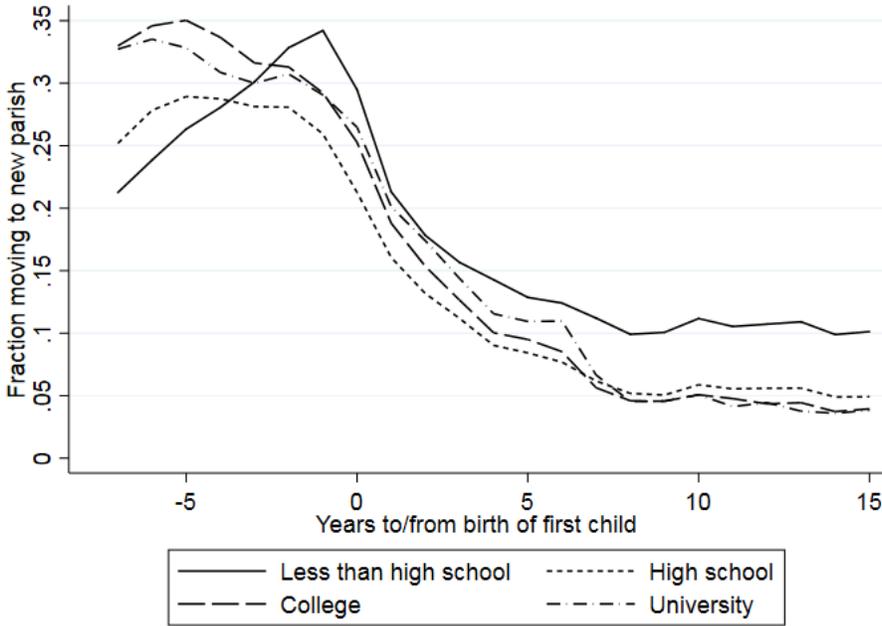
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Formation**

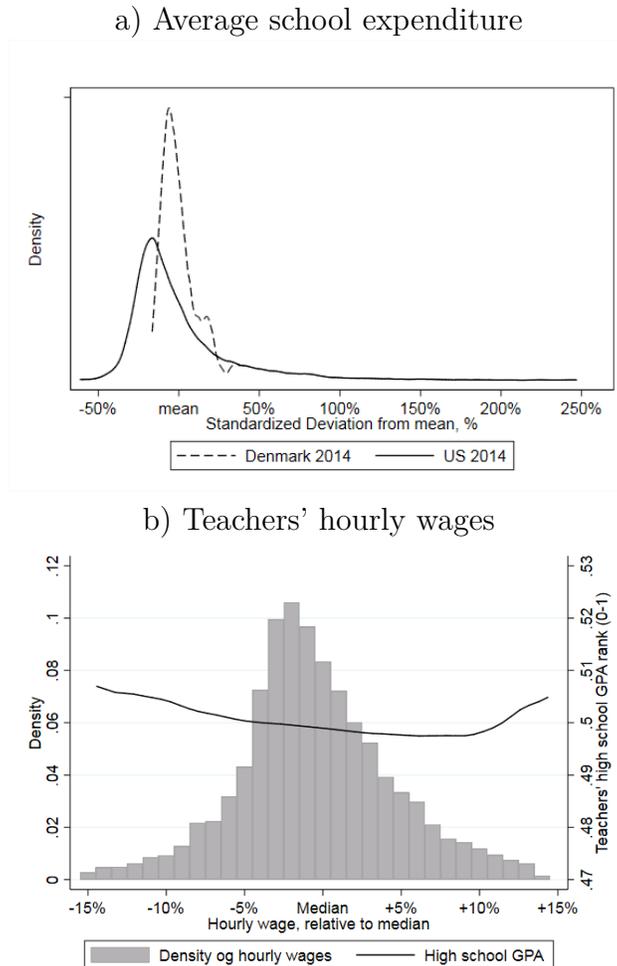
A Additional Figures and Tables

Figure A.1: Stability of Residential Choice: Fraction Moving Each Year by Time to/from Birth of First Child and Mother’s Education



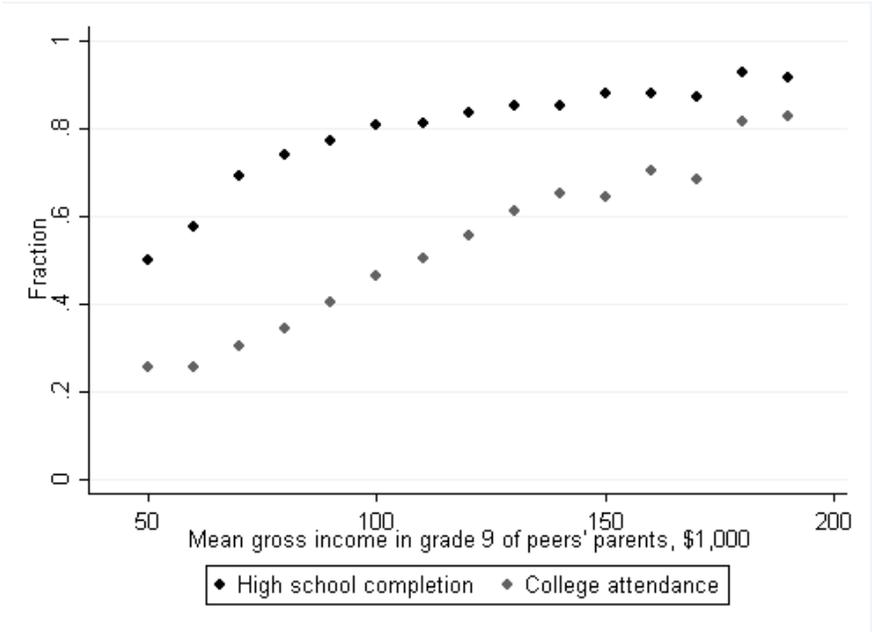
Note: Reprint from [Cholli et al. \(2020\)](#). The figure shows the fraction of mothers moving to a new parish (regions around half the size of the average census-tract), by mothers’ education and time to/from the birth of her first child. Full population register data form cohorts born 1991-1995. Note that school start is at age 7 for the cohorts in question (i.e. the year after the downward kink in the middle of the figure).

Figure A.2: Average Public School Expenditures in Denmark and the U.S.



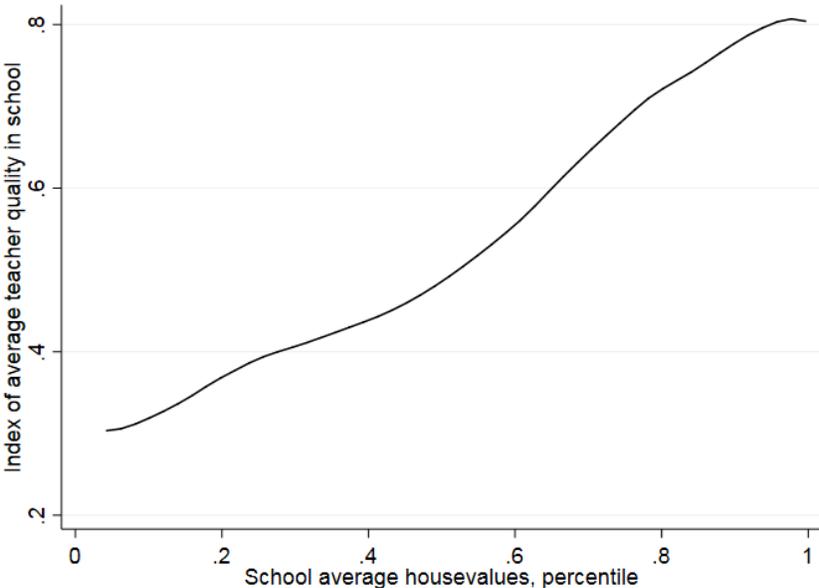
Note: Figure a) shows average per pupil school expenditures in public schools in 2014 relative to the country average. Source: Denmark: www.statistikbanken.dk (Statistics Denmark); U.S.: Annual Survey of School System Finances; <https://catalog.data.gov/dataset/annual-survey-of-school-system-finances>. Figure b) shows the distribution of teachers' hourly wage rates in 2014 as a percentage deviation from the median wage rate. The figure also presents the association between teachers' rank of high school GPA and hourly wages (note that the y-axis only spans from 0.47–0.53; $\text{corr}(\text{wage}, \text{testscore}) = -0.03$, with $p = 0.73$ for H_0 that $\text{corr} = 0$ and H_A that $\text{corr} \neq 0$). Hourly wage rates are adjusted for years of experience to remove variation stemming from the wage-progression at different levels of experience set by collective bargaining. This adjustment involves some measurement error, as it uses *years since graduation* and not *years of employment as a teacher in a Danish municipality*. Also, the hourly wage rates are not adjusted for the roughly 5% wage differences across regions (a PPP adjustment).

Figure A.3: Average Child High School Completion and College Attendance by School-Peers' Family Income



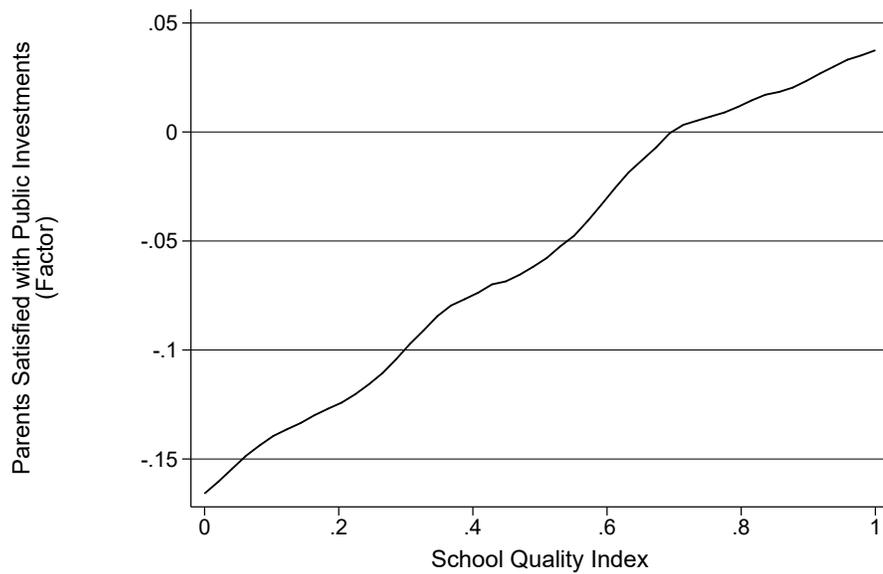
Note: The figure reprints Figure 12 from [Landersø and Heckman \(2016\)](#) showing average high school completion and college attendance rates across the average of school peers' family income.

Figure A.4: Average Estimated School Quality across Property Values in Catchment Area



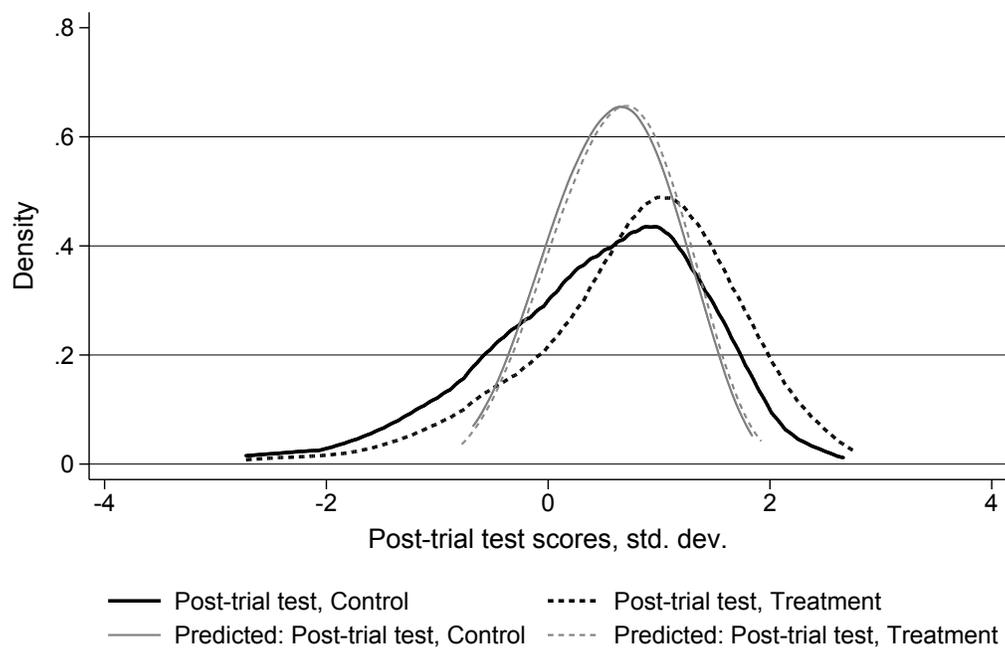
Note: The figure shows the average estimated teacher quality percentile in schools across the average property value in the school catchment area ranked from lowest average values to highest. To proxy average teacher quality in a given school, we use a unique link between all school teachers in Denmark, the schools they work in, and the children who attend those schools. The multiple dimensions of teacher characteristics are condensed to an index ranging from 0 (the lowest quality teacher by observable characteristics) to 1 (the highest quality teacher).

Figure A.5: Parents' Satisfaction with Teaching by School Quality



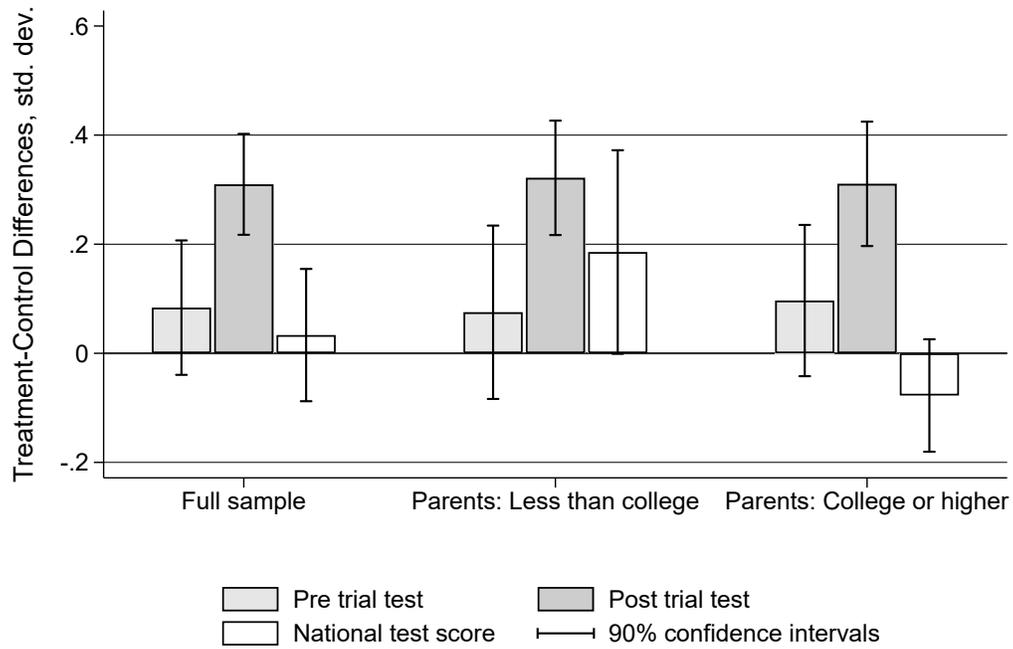
Note: The figure shows the association between parents' satisfaction with public investments (std. dev. standardized to 1, see details on the factor analysis in Section C.4) with school quality (described in Section 4). Fit estimated with kernel-weighted local polynomial smoothing.

Figure A.6: Actual and Predicted Test Score Distributions



Note: The figure shows the actual post-trial test score distribution by treatment status (black lines) and predictions from regression results: $y_i = X_i'\beta$ (grey lines). See table 2 for a full list of the included covariates and Table A.3 for the mean differences in predicted test scores.

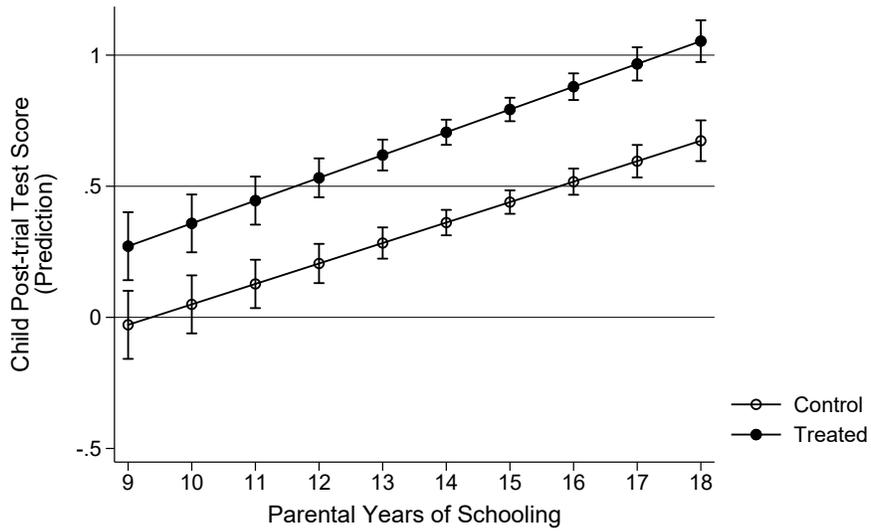
Figure A.7: Treatment-Control Differences, Pre-Trial, Post-Trial, and Grade 2, Conditional on Covariates



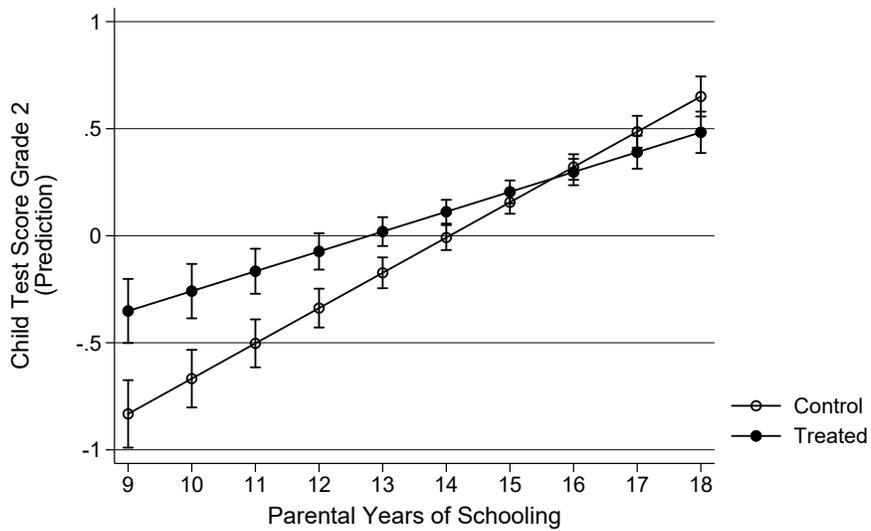
Note: The figure mimics Fig. 5, but presents estimates conditional on all covariates in Table 2, including pre-trial test scores for regressions of post-trial and grade 2 language test scores. We plot treatment–control differences (β_t) in test scores y_{it} from $y_{it} = \alpha + \beta_t T_i + X' \delta_t + \varepsilon_{it}$ with 90% confidence intervals on the treatment indicator. Standard errors are clustered at the preschool level.

Figure A.8: Association Between Child Skills and Parent' Education by Treatment Status

a) Post-trial Test Scores (Preschool)

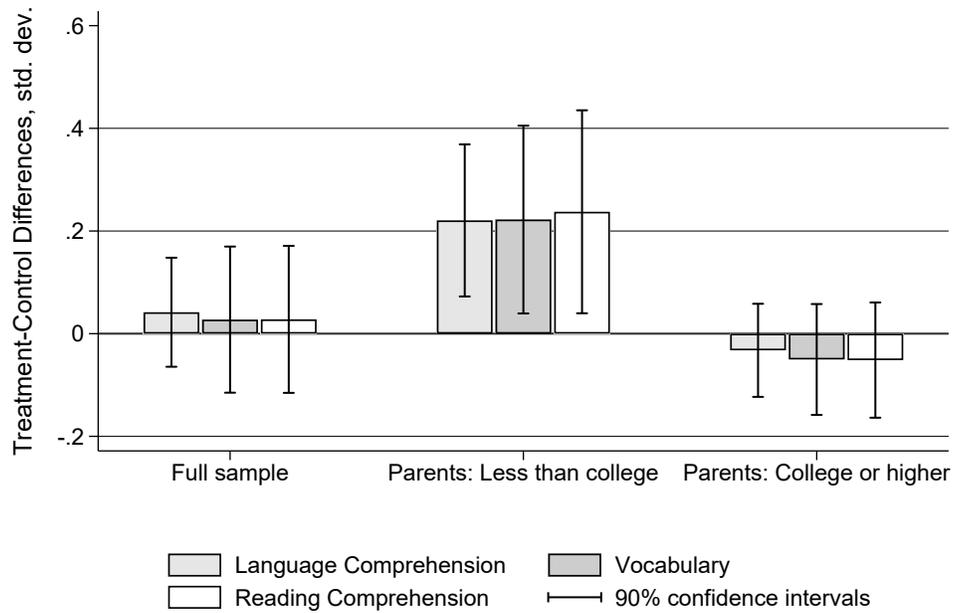


b) Test Scores 2nd Grade (School)



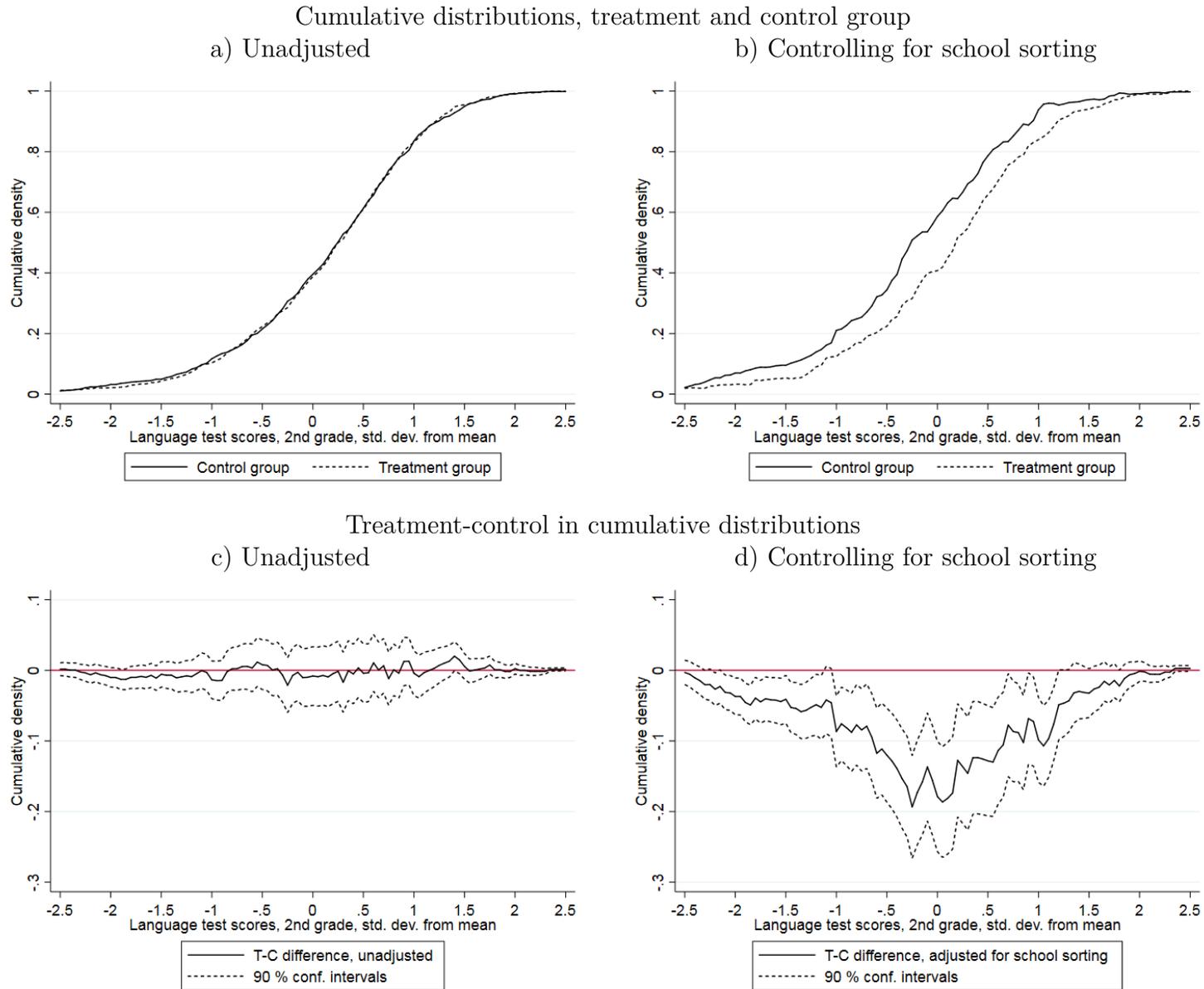
Note: The figure shows the predicted post-trial and grade 2 language test scores from regressions where a linear term for parental highest years of education has been interacted with a treatment indicator along with the 90% confidence intervals. Standard errors are clustered at the preschool level.

Figure A.9: Treatment-Control Differences in Grade 2 by Language-Skill Dimension and Parental Education



Note: The figure plots the estimated treatment-control differences in children's test scores with 90% confidence intervals separately for grade 2 language test score subscales. Standard errors are clustered at the preschool level.

Figure A.10: Cumulative distribution of language test scores, 2nd grade



Note: The figure plots the estimated cumulative grade 2 language test score distributions as described by Eq. (17). The estimates are computed by using as outcomes dummy variables indicating whether test scores y are below or equal to a threshold $y \leq x$, and then running regressions varying x from -2.5 to $+2.5$ std. dev. Figures (a) and (b) plot estimates of $\alpha + \beta$ and $\bar{\alpha} + \bar{\beta}$, respectively. Figures (c) and (d) plot estimates of β and $\bar{\beta}$, respectively. Standard errors are clustered at the preschool level.

Table A.1: Treatment-Control Differences by Outcome and Sample

	Post-Trial Test			Test scores		
	unrestricted	panel DNT	panel+survey	unrestricted	panel DNT	panel+survey
Treated	0.342*** (0.083)	0.386*** (0.101)	0.399*** (0.105)	0.040 (0.085)	0.040 (0.085)	0.009 (0.085)
Observations	2300	1562	951	1562	1562	951

Note: The table shows estimated treatment-control differences for three sample definitions. The “unrestricted” sample uses all available children in the sample at each age. The “panel DNT” restricts the sample to only children for whom grade 2 test scores are available (as the grade 2 test scores for the youngest cohort in the data are not available yet). “panel+survey” sample restricts the sample to all for whom the grade 2 tests scores are available, as well as the parent responses for the follow-up survey. Standard errors are clustered at the preschool level. Standard errors in parenthesis, + ($p < 0.1$), * ($p < 0.05$), ** ($p < 0.01$), *** ($p < 0.001$).

Table A.2: Children’s Test Scores by Estimated School Quality Deciles

Decile	10th percentile	Average	90th percentile
1	-1.38	-0.55	0.34
2	-1.28	-0.35	0.53
3	-1.13	-0.24	0.58
4	-1.00	-0.16	0.64
5	-0.88	-0.09	0.68
6	-0.89	-0.06	0.72
7	-0.73	0.04	0.81
8	-0.66	0.15	0.87
9	-0.59	0.29	1.13
10	-0.41	0.47	1.29

Note: The table shows the 10th percentile, average, and 90th percentile of school average test scores by deciles of estimated school quality proxied by teacher’s observable characteristics. Test scores have been standardized to mean 0 and standard deviation 1 at year and grade level. The table is based on 5,557 school by year observations and 1,526,234 observations of children’s standardized test scores.

Table A.3: Joint Test of Balance by Treatment Status

	(1)	(2)	(3)
	All	Less than college	College or higher
Pre-Trial Test Score	0.024 (0.020)	0.025 (0.025)	0.026 (0.023)
Age	0.027 (0.040)	-0.015 (0.050)	0.059 (0.052)
Born in 2007	-0.058 (0.092)	0.216 (0.138)	-0.224 ⁺ (0.126)
Born in 2008	-0.007 (0.060)	0.159 ⁺ (0.093)	-0.115 (0.078)
Born in 2009	0.041 (0.042)	0.148* (0.068)	-0.030 (0.059)
Born in 2010	0.000 (.)	0.000 (.)	0.000 (.)
Boy	-0.026 (0.026)	-0.050 (0.034)	-0.011 (0.034)
Child's birth weight, kg	-0.055* (0.027)	-0.093* (0.040)	-0.027 (0.037)
Gestation length, weeks	0.000 (0.009)	-0.012 (0.012)	0.004 (0.012)
Apgar score	0.018 (0.021)	-0.002 (0.033)	0.026 (0.024)
Number of siblings	-0.019 (0.020)	-0.028 (0.028)	-0.020 (0.022)
Mother's weight, kg.	0.001 (0.001)	-0.000 (0.001)	0.002 ⁺ (0.001)
Mother's age, 2015	0.003 (0.004)	0.008 (0.006)	-0.002 (0.005)
Mother's years of schooling	-0.005 (0.008)	-0.004 (0.015)	-0.002 (0.009)
Mother employed in 2012	0.036 (0.037)	0.054 (0.051)	-0.003 (0.047)
Father's years of schooling	-0.002 (0.009)	-0.006 (0.012)	0.004 (0.011)
Father's age, 2015	-0.005 (0.003)	-0.002 (0.005)	-0.006 (0.004)
Father employed in 2012	-0.012 (0.052)	-0.021 (0.063)	0.025 (0.061)
Household Income	0.000 (0.000)	-0.000 (0.001)	0.000 (0.000)
Constant	0.396 (0.656)	1.313 (0.800)	-0.135 (0.872)
Observations	2300	838	1462

Note: The table shows regression results from outcomes y_i regressed on covariates. The pre-trial test score is standardized to mean zero and standard deviation one within each test score measure from the two interventions. The estimates shown are from regressions by intervention, not conditioning on the other covariates being present at the same time. The estimation sample includes all children for whom pre- and post-test scores were available. "Household Inc" stands for household income measured in 1,000 USD of the year 2010. Standard errors in parentheses. ⁺($p < 0.1$), * ($p < 0.05$), ** ($p < 0.01$), *** ($p < 0.001$).

Table A.4: Treatment-Control Differences, Heterogeneity by Parent’s Education

	Pre-Trial Test		Post-Trial Test		Test Grade 2	
	(1) Less than college	(2) College or higher	(3) Less than college	(4) College or higher	(5) Less than college	(6) College or higher
Treatment	0.080 (0.093)	0.090 (0.093)	0.349*** (0.088)	0.354*** (0.091)	0.260** (0.109)	-0.051 (0.064)
Observations	836	1462	836	1462	597	963
Pretest	No	No	No	No	No	No
Covariates	No	No	No	No	No	No
Mean (control)	-0.305	0.110	0.242	0.539	-0.294	0.384

Note: The table shows the estimates corresponding to Fig. 5 in main text. “Low ed” is the subsample of parents who have less than 14 years of education, labeled “Less than college” in the main text, and “high ed” is given by parents with “College or higher.” The average of the dependent variable *among children in the control group*, by parental education, is given in “Mean (control).” Standard errors in parentheses. *($p < 0.10$), ** ($p < 0.05$), *** ($p < 0.01$).

Table A.5: Treatment-Control Differences, Heterogeneity by Child’s Pre-Trial Test Scores

	<i>Pre-trial language score</i>		
	Q1	Q2	Q3
Treatment	0.003 (0.936)	-0.006 (0.813)	0.043 (0.263)
Observations	830	711	759
	<i>Post-trial language score</i>		
	Q1	Q2	Q3
Treatment	0.379*** (0.000)	0.348*** (0.000)	0.222* (0.033)
Observations	830	711	759
	<i>2nd grade language score</i>		
	Q1	Q2	Q3
Treatment	0.073 (0.583)	-0.001 (0.988)	-0.074 (0.500)
Observations	559	530	454
Covariates	No	No	No

Note: The table shows estimates corresponding to Table A.4 but by the child’s own pre-trial test score terciles - referenced by “Q1” to “Q3”. p-values in parentheses. * ($p < 0.10$), ** ($p < 0.05$), *** ($p < 0.01$).

Table A.6: Treatment-Control Differences in Parents' Behavior, Heterogeneity by by Parents' Education

	(1) Parental Investment Factor	(2) School Quality	(3) Hours worked/day
Treated × High school or less	0.188* (0.097)	-0.013 (0.027)	-0.245 (0.200)
Treated × College or more	0.125* (0.066)	-0.073*** (0.020)	0.136 (0.135)
High school or less	0.000 (.)	0.000 (.)	0.000 (.)
College or more	0.277*** (0.085)	0.276*** (0.024)	0.502*** (0.175)
Constant	-0.265*** (0.071)	0.355*** (0.020)	6.468*** (0.146)
Observations	1336	1382	1360
Covariates	No	No	No
Mean Dep.var., High school or less	-.165	.348	6.34
Mean Dep.var., College or more	.076	.596	7.04

Note: The table shows estimated treatment-control differences in parents' investments decisions as presented in Fig. 6 in main text. The average of the dependent variable by parental education is given in "Mean Dep.var." The treatment effects are statistically significantly different between parental educationl groups for school quality (p-value 0.07), but not parental investments and borderline for the work hours (p-value .11). Standard errors in parentheses. *($p < 0.10$), ** ($p < 0.05$), *** ($p < 0.01$).

B Technical Appendix

B.1 The General Model

This appendix formally derives the main results presented in Section 2.

The technology of skill formation we use begins with a standard production function for univariate end-of-period skills θ_t that includes self-productivity from θ_{t-1} and investments I_t :

$$\theta_t = j(\theta_{t-1}, I_t) \tag{B.1}$$

Investment is itself a function of parental direct investments P_t and skill investments via the institutional setting, or public G_t , where parents shape $P_t = p(x_t, \theta_P)$ through direct time investments x_t , of which the efficacy depends on their own skills θ_P :

$$I_t = m(p(x_t, \theta_P), g(\underline{G}, \kappa Y_t, e_t, \theta_P)), \tag{B.2}$$

Skill investments via the institutions G_t are a function $g()$ of parental quality and three levels of investment margins: The average level of public institutions, \underline{G} , which parents take as given. Institutional investments depend also on selection into neighborhoods, which is paid for by fraction κ of parents' income, and differences in school quality within neighborhoods. Parents influence public investments G_t through the two last channels, where they select into neighborhoods through spending income, and they select into schools within neighborhoods through spending time on school choice e_t .

$$G_t = g(\underline{G}, \kappa Y_t, e_t, \theta_P), \quad t \in \{1, 2\} \tag{B.3}$$

Before we continue with the model and the derivations, we briefly pause to motivate the use e_t . In the main text we provide evidence of and discuss how parents can sort even within a given neighborhood (i.e., additional sorting possibilities that does not originate from income). This could for example occur via exploring the quality of schools (via publicly

available records or from visiting schools), contacting administrative personnel in charge of slots in preschools or schools. We do not posit that e in absolute terms is as large as x or h , only that this effort also affects realized school quality. Furthermore, in essence e is simply an input into institutional sorting that has the same opportunity costs in terms of foregone leisure as time spent on home-investments (x). While labor supply h has the same effect in terms of increasing institutional investments at the expense of leisure, labor supply also enters utility through effects on consumption. Hence, the intuition is clearer when we focus on e as it allows us to distill parents' tradeoff when balancing home and institutional investments.

Parents receive an hourly wage w for their labor h_t , where w is a function ω of their quality. Thus, income depends on $w = \omega(\theta_P)$, and time spent working h_t .

$$Y_t = h_t w, \quad t \in \{1, 2\} \tag{B.4}$$

Parents thus spend all their available time of 1 on work, direct investments, school selection, or leisure l_t :

$$1 = h_t + x_t + e_t + l_t \quad \text{for } t \in \{1, 2\} \tag{B.5}$$

If we consider a two-period model, parental **utility** is the following function of parental consumption and children's future skills:

$$U(c_1, c_2, l_1, l_2, \theta_2) = u_1(c_1, l_1) + \beta u_2(c_2, l_2) + \beta^2 V(\theta_2) \tag{B.6}$$

where β is the discount factor. **Without borrowing**, parents' budget constraints each period are:³⁹

$$c_1 = (1 - \kappa)Y_1 \tag{B.7}$$

$$c_2 = (1 - \kappa)Y_2$$

³⁹Below we will also consider the case where parents can borrow freely at the same rate as implied by the discount factor β .

Parents then maximize their utility, subject to time and budget constraints and the technology described in Eqs. (B.1) to (B.3). The Lagrangian for this problem (ignoring the non-negativity constraints on time use) is

$$\begin{aligned}
\mathcal{L}_{c_1, c_2, h_1, h_2, x_1, x_2, e_1, e_2} &= u_1(c_1, l_1) + \beta u_2(c_2, l_2) + \beta^2 V(\theta_2(\theta_1(\theta_0, I_1), I_2)) \\
&+ \lambda_1(h_1 w(1 - \kappa) - c_1) \\
&+ \lambda_2(h_2 w(1 - \kappa) - c_2) \\
&+ \lambda_3(1 - h_1 - x_1 - e_1 - l_1) \\
&+ \lambda_4(1 - h_2 - x_2 - e_2 - l_2)
\end{aligned}$$

B.1.1 General first order conditions in absence of a shock to public quality

The First order conditions are

$$\frac{\partial \mathcal{L}}{\partial c_1} : \quad \frac{\partial u_1}{\partial c_1} = \lambda_1 \quad (\text{FOC}.c_1)$$

$$\frac{\partial \mathcal{L}}{\partial c_2} : \quad \beta \frac{\partial u_2}{\partial c_2} = \lambda_2 \quad (\text{FOC}.c_2)$$

$$\frac{\partial \mathcal{L}}{\partial l_1} : \quad \frac{\partial u_1}{\partial l_1} = \lambda_3 \quad (\text{FOC}.l_1)$$

$$\frac{\partial \mathcal{L}}{\partial l_2} : \quad \beta \frac{\partial u_2}{\partial l_2} = \lambda_4 \quad (\text{FOC}.l_2)$$

$$\frac{\partial \mathcal{L}}{\partial x_1} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial P_1} \frac{\partial P_1}{\partial x_1} = \lambda_3 \quad (\text{FOC}.x_1)$$

$$\frac{\partial \mathcal{L}}{\partial x_2} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2} = \lambda_4 \quad (\text{FOC}.x_2)$$

$$\frac{\partial \mathcal{L}}{\partial e_1} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial e_1} = \lambda_3 \quad (\text{FOC}.e_1)$$

$$\frac{\partial \mathcal{L}}{\partial e_2} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial e_2} = \lambda_4 \quad (\text{FOC}.e_2)$$

$$\frac{\partial \mathcal{L}}{\partial h_1} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial h_1} + \lambda_1 w(1 - \kappa) = \lambda_3 \quad (\text{FOC}.h_1)$$

$$\frac{\partial \mathcal{L}}{\partial h_2} : \quad \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial h_2} + \lambda_2 w(1 - \kappa) = \lambda_4 \quad (\text{FOC}.h_2)$$

$$\frac{\partial \mathcal{L}}{\partial \lambda_1} : \quad h_1(1 - \kappa)w = c_1 \quad (\text{FOC}.\lambda_1)$$

$$\frac{\partial \mathcal{L}}{\partial \lambda_2} : \quad h_2(1 - \kappa)w = c_2 \quad (\text{FOC}.\lambda_2)$$

$$\frac{\partial \mathcal{L}}{\partial \lambda_3} : \quad h_1 + x_1 + e_1 + l_1 = 1 \quad (\text{FOC}.\lambda_3)$$

$$\frac{\partial \mathcal{L}}{\partial \lambda_4} : \quad h_2 + x_2 + e_2 + l_2 = 1 \quad (\text{FOC}.\lambda_4)$$

It immediately follows from Eqs. (FOC. x_1) to (FOC. e_2) that

$$\begin{aligned}
\frac{\partial V(\theta_2)}{\partial x_t} &= \frac{\partial V(\theta_2)}{\partial e_t} \\
\leftrightarrow \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_t} \frac{\partial I_t}{\partial P_t} \frac{\partial P_t}{\partial x_t} &= \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_t} \frac{\partial I_t}{\partial G_t} \frac{\partial G_t}{\partial e_t} \\
\leftrightarrow \frac{\partial I_t(P_t, G_t)}{\partial P_t} \frac{\partial P_t(x_t, \theta_P)}{\partial x_t} &= \frac{\partial I_t(P_t, G_t)}{\partial G_t} \frac{\partial G_t(\underline{G}, \kappa Y_t, e_t, \theta_P)}{\partial e_t} \quad \text{for } t \in \{1, 2\} \quad (\text{B.8})
\end{aligned}$$

Note that this equality between the productivities of parental investments via direct time spent with children (x_t) and via institutional selectivity (e_t) is a very general result that holds in both periods, and which does not depend on the possibility of borrowing or the budget constraints. It results simply from the condition that in optimality, parents must be indifferent between how to invest time in their children’s skill formation.

In fact, Eq. (B.8) is a general result for any within-period (not just two as we consider here) optimization **only assuming that functions are twice differentiable and $I()$ is increasing in P and G , and $p()$ and $g()$ increasing in x_t and e_t , respectively.**

B.1.2 Marginal Rate of Technical Substitution

Rewriting Eq. (B.8), it becomes evident that in each period, the marginal rate of technical substitution in the “production” of I between home and institutional investments is given by:

$$|\text{MRTS}(P_t, G_t)| = \frac{\partial I(P_t, G_t)/\partial P_t}{\partial I(P_t, G_t)/\partial G_t} = \frac{\partial g(\underline{G}, \kappa Y_t, e_t, \theta_P)/\partial e_t}{\partial p(x_t, \theta_P)/\partial x_t}, \quad t \in \{1, 2\} \quad (\text{B.9})$$

This formulation highlights the close link between the “outer” production function for investments, $I(P, G)$, and the “inner” production functions for parental and institutional-specific investments as they depend on parental time investments in terms of direct investments x_t and school choice activities e_t . It becomes evident that assumptions about how P_t and G_t interact in producing overall investments I_t immediately have implications for the micro-foundations of these sub-types of investments by parental time e_t and x_t . The productivities

of investments at home and in the institutional setting are inherently linked at the “outer” and “inner” parts of the production functions. For example, when assuming a Cobb-Douglas production technology for I_t , shaping the ratio of $\frac{\partial I_t}{\partial P_t} / \frac{\partial I_t}{\partial G_t}$ limits the possible production functions for how parental time uses shape P_t and G_t individually, influencing $\frac{\partial P_t}{\partial x_t} / \frac{\partial G_t}{\partial e_t}$.

Equation B.9 states that the marginal rate of technical substitution (MRTS) between home and institutional investments as inputs in total investments in human capital formation must equal the ratio between the marginal productivity of parents’ time spent on investments at home and in an institutional setting.

As the opportunity costs of increasing x and e are identical, it must hold that if parents choose time inputs in home investments at a level where additional time spent at home would increase home investments P more than a similar change in e would increase institutional investments G , then it must be because the marginal return to home investments P in total investments I is lower than the marginal return to institutional investments G in total investments I .

Fig. B.1 presents a graphical illustration of the intuition. Fig. B.1a shows the isoquant between home and institutional investments, and the associated MRTS (the tangent). The tangent in Fig. B.1a must equal to ratio between the two marginal products of time spent at home and on institutional sorting, illustrated in Figs. B.1b and B.1c.

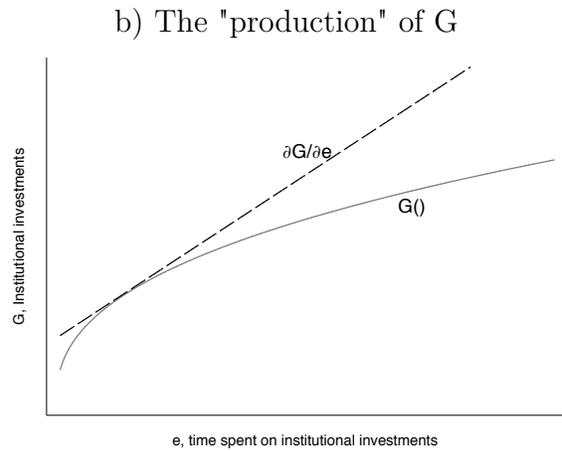
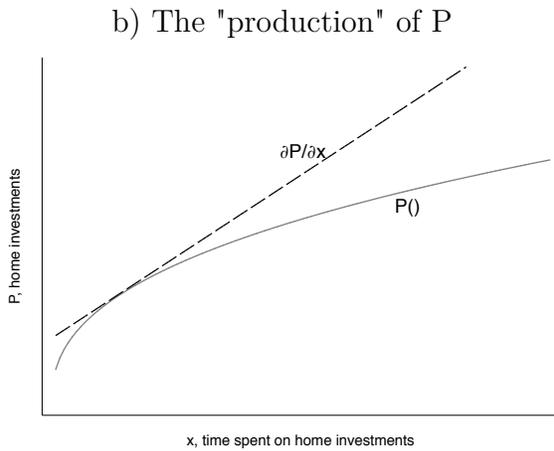
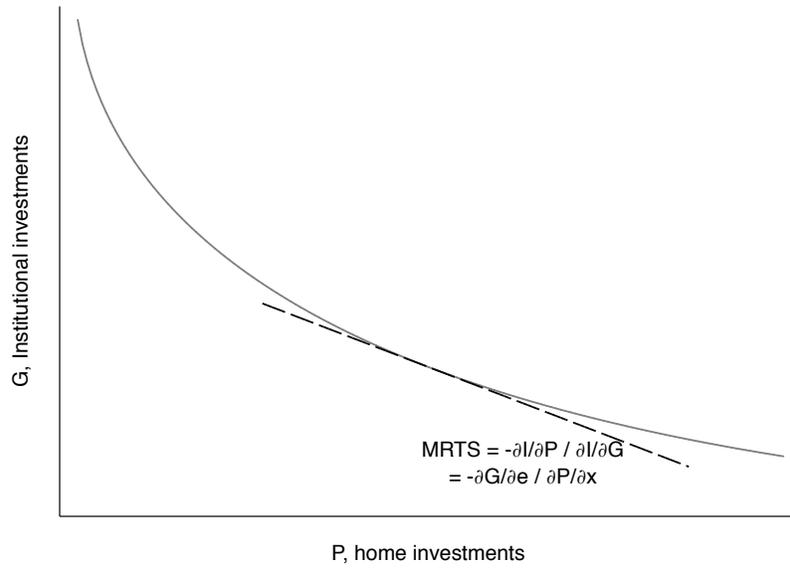
The elasticity of substitution between P and G is then given by:

$$\varepsilon_{P,G} = \left[\frac{\partial \text{MRTS}(P,G)}{\partial (P/G)} \frac{P/G}{\text{MRTS}(P,G)} \right]^{-1} \quad (\text{B.10})$$

The second term of the product in Eq. (B.10) will always be positive (because we have assumed that both e_t and x_t are always strictly productive in their respective investment functions). Therefore, whether P and G are substitutes or complements in the “production” of investments (i.e., whether $\varepsilon_{P,G}$ is positive or negative), depends on the sign of the first term, which relates a change in the MRTS to an underlying change in the ratio of parental to public investments (P/G). This is useful to analyze what happens when institutional

Figure B.1: Optimal choices of G and P

a) Marginal Rate of Technical Substitution between the two investment types



Note: The figure illustrates the marginal rate of technical substitution (MRTS) between home and institutional investments, and how this relates to the marginal product of time spent on home investments and institutional investments (through e.g., sorting). For illustrative purposes, a) is constructed from a CES function with an elasticity of substitution of 0.5, while both home and institutional investments in b) and c) are drawn as having concave production functions.

investments increase because public quality (\underline{G}) increased. This would initially lower P/G . From Eq. (B.9), we have that $-\text{MRTS}(P_t, G_t) = \frac{\partial g}{\partial e_t} / \frac{\partial p}{\partial x_t}$, which implies that the elasticity of substitution between home and institutional investments depends on the slopes of $g()$ and $p()$ as a function of e_t and x_t . Thus, if it is observed (at current levels of P and G) that home and institutional investments are *substitutes* ($\varepsilon_{P,G} > 0$), then $\partial \text{MRTS}(P_t, G_t) / \partial (P/G)$ must be positive. Note that this analysis has to factor in parental responses to both e_t and x_t , as they together produce the elasticity. If the increase in \underline{G} even after parental adjustments leads to a decrease in P/G , the marginal productivity of $g()$ with respect to e_t must fall relative to the marginal productivity of $p()$ with respect to x_t . If home and institutional investments are complements,⁴⁰ the first term of Eq. (B.10) has to be negative. The joint changes of e_t and x_t , and how these changes investments in the home and institutional setting, will inform us of the sign of the elasticity of substitution. We will return to this key result below.

Another set of noteworthy equilibrium conditions are the following expressions that relate the marginal utilities of the available parental time uses:

$$\frac{\partial u_1}{\partial l_1} = \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial P_1} \frac{\partial P_1}{\partial x_1} \quad (\text{B.11})$$

$$\begin{aligned} &= \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial e_1} \\ \frac{\partial u_1}{\partial l_1} &= \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial h_1} + \frac{\partial u_1}{\partial c_1} w(1 - \kappa) \end{aligned} \quad (\text{B.12})$$

$$\frac{\partial u_2}{\partial l_2} = \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2} \quad (\text{B.13})$$

$$\begin{aligned} &= \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial e_2} \\ \frac{\partial u_2}{\partial l_2} &= \beta \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial h_2} + \frac{\partial u_2}{\partial c_2} w(1 - \kappa) \end{aligned} \quad (\text{B.14})$$

In equilibrium, parents must be indifferent in allocating their time to additional leisure (giving direct utility), direct investments in children or via school choice (giving indirect utility through future child skills), or labor (allowing greater consumption for direct utility

⁴⁰Naturally, the elasticity of substitution can vary along the production possibility frontier. We will consider the specific conclusions from a CES function below.

or improving neighborhood public goods that raise future child skills).

B.1.3 Allowing borrowing in general model

With free borrowing at an interest rate of $r = 1/\beta - 1$, the previous first order conditions all remain except for Eq. (FOC. λ_1) and Eq. (FOC. λ_2), and there will be added one first order condition for borrowing amount B . The latter one will imply $\lambda_1 = \frac{1}{\beta}\lambda_2$, which immediately yields an additional across-period equilibrium condition of

$$\frac{\partial u_1}{\partial c_1} = \frac{\partial u_2}{\partial c_2} \tag{B.15}$$

To arrive at more direct implications of the model, we will have to introduce further restrictions.

B.2 The specific model: early residential choice and borrowing

A central part of the model is how parents' can influence the institutional investments. One way to do so is through residential choices. However, this is not completely flexible in practice, and empirically it is observed that most families settle with their children before the child starts school (see Section 5 in the main text, Fig. A.1 in the appendix, and Cholli et al., 2020). We therefore introduce a change with respect to the above set-up that renders the parents' decision problem more realistic, such that parents do not move between the various schooling stages of their children.

B.2.1 Introducing lock-in of early residential choices

We let the neighborhood quality be determined by *initial* parental income in period 1, not re-optimized each period. This alters the budget constraint, where neighborhood expenditures are fixed at $\kappa w h_1$, and h_1 influences on θ_2 not only via G_1 and thus θ_1 , but also via public

quality G_2 .

$$\begin{aligned} c_1 + \kappa Y_1 &= Y_1 & \Leftrightarrow c_1 &= h_1(1 - \kappa)w & \text{(B.16)} \\ c_2 + \kappa Y_1 &= Y_2 & \Leftrightarrow c_2 &= h_2w - h_1\kappa w \end{aligned}$$

The Lagrangian for the more realistic problem changes to

$$\begin{aligned} \mathcal{L}_{c_1, c_2, h_1, h_2, x_1, x_2, e_1, e_2} &= u_1(c_1, l_1) + \beta u_2(c_2, l_2) \\ &+ \beta^2 V(\theta_2(\theta_1(\theta_0, I_1), I_2)) \\ &+ \lambda_1(h_1w(1 - \kappa) - c_1) \\ &+ \lambda_2(h_2w - h_1\kappa w - c_2) \\ &+ \lambda_3(1 - h_1 - x_1 - e_1 - l_1) \\ &+ \lambda_4(1 - h_2 - x_2 - e_2 - l_2) \end{aligned}$$

using the same technology as above, and as there not allowing borrowing across periods.

The altered **First order conditions** (relative to the general model of Section B.1) are

$$\frac{\partial \mathcal{L}}{\partial h_1} : \beta^2 \frac{\partial V}{\partial \theta_2} \left[\frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial h_1} + \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial h_1} \right] + \lambda_1 w(1 - \kappa) - \lambda_2 \kappa w - \lambda_3 = 0 \quad \text{(B.17)}$$

$$\frac{\partial \mathcal{L}}{\partial h_2} : \lambda_2 w = \lambda_4 \quad \text{(B.18)}$$

$$\frac{\partial \mathcal{L}}{\partial \lambda_2} : h_2 w - h_1 \kappa w = c_2 \quad \text{(B.19)}$$

The equilibrium conditions of the previous section are maintained (Eq. (B.8), Eq. (B.11) and Eq. (B.13)), except for Eq. (B.12) and Eq. (B.14), where specifically the latter becomes

$$\frac{\partial u_2}{\partial l_2} = w \frac{\partial u_2}{\partial c_2}. \quad \text{(B.20)}$$

The first order conditions can be further combined **if we assume a specific restriction on $g(\cdot)$** of Eq. (B.2) (but without losing generality), that within the function for investments from the institutional setting, the marginal productivity of parental labor time is proportional to

the marginal productivity of time spent on school sorting:

$$\frac{\partial g_1}{\partial h_1} = \frac{\partial g_1}{\partial e_1} \kappa w \quad (\text{B.21})$$

$$\frac{\partial g_2}{\partial h_1} = \frac{\partial g_2}{\partial e_2} \kappa w \quad (\text{B.22})$$

This allows us to rewrite Eq. (B.17) as follows, because $\beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial h_1} = \kappa w \lambda_3$ in Eq. (FOC.e₁), and $\beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial G_2} \frac{\partial G_2}{\partial h_1} = \kappa w \lambda_4$ in Eq. (FOC.e₂):

$$\kappa w \lambda_3 + \kappa w \lambda_4 + \lambda_1(1 - \kappa)w = \lambda_2 \kappa w + \lambda_3$$

$$\lambda_2 \kappa w(w - 1) + \lambda_1(1 - \kappa)w = \lambda_3(1 - \kappa w) \quad \text{using Eq. (B.18)}$$

Adding to this last expression equations FOC.c₁, FOC.c₁, and FOC.l₁, we get that the marginal utility of labor in period 1 is a function of both marginal utility of consumption in period 1 and 2.

$$\frac{\partial u_1}{\partial c_1}(1 - \kappa)w - \frac{\partial u_2}{\partial c_2} \kappa w(1 - w) = \frac{\partial u_1}{\partial l_1}(1 - \kappa w), \quad (\text{B.23})$$

which reflects that residential choice today affects future residential choice and thereby also future expenses to housing and what fraction of income that is left for consumption. The consequence is that period 1 labor supply will be increased to a higher point than it would otherwise have been (i.e. parents are going to work more than they would otherwise have done when the child is young).

B.2.2 Introducing Free Borrowing

When we additionally **allow for free borrowing** at interest rate $r = 1/\beta - 1$ (but not allowing parents to leave positive or negative financial bequests), the new budget constraints in each period are

$$\begin{aligned} c_1 &= (1 - \kappa)Y_1 + B \\ c_2 &= (1 - \kappa)Y_2 - \frac{1}{\beta}B \end{aligned}$$

and Eq. (B.23) changes to:

$$\lambda_1 [(1 - \kappa)w + \beta\kappa w(w - 1)] = \lambda_3(1 - \kappa w) \quad \text{using that } \lambda_1 = \lambda_2/\beta \text{ when allowing for borrowing}$$

$$\lambda_1 w d_w = \lambda_3 \quad \text{defining } d_w \equiv \frac{1 - \kappa - (1 - w)\beta\kappa}{1 - \kappa w} \quad (\text{B.24})$$

The denotation of constant d_w is to serve as a reminder that it is a function of parental earnings w , which reflect parental quality θ_P . Adding the FOCs for consumption and leisure, it can be shown that

$$w d_w \frac{\partial u_1}{\partial c_1} = \frac{\partial u_1}{\partial l_1} \quad (\text{B.25})$$

This corresponds to period 2, where the marginal utility of consumption must equal the marginal utility of leisure (combining Eqs. (B.18), (FOC.c₂) and (FOC.l₂)):

$$w \frac{\partial u_2}{\partial c_2} = \frac{\partial u_2}{\partial l_2} \quad (\text{B.26})$$

Rewriting Eq. (B.24) further proves quite useful. Using the FOCs for B and h_2 , which result in $\lambda_1 = \frac{1}{\beta}\lambda_2 = \frac{1}{\beta w}\lambda_4$, we obtain $\frac{d_w}{\beta}\lambda_4 = \lambda_3$. This allows us to combine the FOCs for x_1 and x_2 , and e_1 and e_2 as well as l_1 and l_2 :

$$w d_w \frac{\partial u_1}{\partial c_1} = \frac{\partial u_1}{\partial l_1} \quad (\text{B.27})$$

$$= \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial P_1} \frac{\partial P_1}{\partial x_1} \quad (\text{B.28})$$

$$= \beta^2 \frac{\partial V}{\partial \theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial I_1} \frac{\partial I_1}{\partial G_1} \frac{\partial G_1}{\partial e_1} \quad (\text{B.29})$$

\Leftrightarrow

$$d_w \frac{\partial u_2}{\partial l_2} = \frac{\partial u_1}{\partial l_1} \quad (\text{B.30})$$

$$\frac{d_w}{\beta} \frac{\partial \theta_2}{\partial x_2} = \frac{\partial \theta_2}{\partial x_1} \quad (\text{B.31})$$

$$\frac{d_w}{\beta} \frac{\partial \theta_2}{\partial e_2} = \frac{\partial \theta_2}{\partial e_1} \quad (\text{B.32})$$

Across periods, parental investments must have equal discounted productivity, weighted with term d_w . These results depend on both the budget constraint with free borrowing for parents within periods 1 and 2, and the specific functional form with proportional productivities of investments via institutional quality through school or neighborhood sorting.

B.3 Inserting functional forms

Let us now specify all functional forms. Given that allowing for borrowing gives rise to interesting across-period equilibrium conditions that correspond to optimal investment paths over time, we now continue with the model of Section B.2, which allows borrowing (which nevertheless leaves the within-period results largely unchanged), and with the lock-in effect of residential choice in period 1. The standard functional form for skill formation can be used as a CES specification:

$$\theta_t = [\gamma\theta_{t-1}^\phi + (1 - \gamma)I_t^\phi]^{1/\phi}, \quad t \in \{1, 2\} \quad (\text{B.33})$$

Note that this specification implies a separability of all investments from previous skills. Investment I_t can similarly be generated by a CES function:

$$I_t = [\pi P_t^\sigma + (1 - \pi)G_t^\sigma]^{1/\sigma}, \quad t \in \{1, 2\} \quad (\text{B.34})$$

This formulation is neutral about whether P_t and G_t are substitutes or complements, allowing $\sigma \in \{1, -\infty\}$. For g , f , and $u(\cdot)$:

$$P_t = (x_t\theta_P)^a, \quad 0 < a < 1 \quad (\text{B.35})$$

$$G_t = (\underline{G} + \kappa wh_1 + e_t)^b, \quad 0 < b < 1 \quad (\text{B.36})$$

$$u(c_t, l_t) = \alpha \ln(c_t) + (1 - \alpha) \ln(l_t) \quad (\text{B.37})$$

$$V(\theta_2) = \nu \ln(\theta_2) \quad (\text{B.38})$$

The above optimality conditions in Eqs. (B.8), (B.13) and (B.20), which result from the

general set-up, become

$$x_t = \left[\frac{a}{b} \frac{\pi}{1-\pi} \theta_P^{a\sigma} (\underline{G} + \kappa w h_1 + e_t)^{1-b\sigma} \right]^{\frac{1}{1-a\sigma}} \quad \text{for } t \in \{1, 2\} \quad (\text{B.39})$$

$$\frac{1-\alpha}{l_2} = \beta \nu \pi a \theta_p \left[\gamma \theta_1^\phi + (1-\gamma) I_2^\phi \right]^{\frac{1}{\phi} - 1 - \phi} \left[\pi P_2^\sigma + (1-\pi) G_2^\sigma \right]^{\frac{1-\sigma}{\sigma}} P_2^{\sigma-1/a} \quad (\text{B.40})$$

$$c_2 = w \frac{\alpha}{1-\alpha} l_2. \quad (\text{B.41})$$

With borrowing across periods and the assumed functional forms, we also obtain the following equilibrium conditions (refer to Eqs. (B.30) to (B.32), and Eq. (B.25), respectively):

$$l_2 = d_w l_1 \quad (\text{B.42})$$

$$\frac{x_1}{x_2} = \left[\frac{\beta \gamma}{d_w} \left(\frac{I_1}{I_2} \right)^{\phi-\sigma} \right]^{\frac{1}{1-a\sigma}} \quad (\text{B.43})$$

$$\frac{G_1}{G_2} = \left[\frac{\beta \gamma}{d_w} \left(\frac{I_1}{I_2} \right)^{\phi-\sigma} \right]^{\frac{1}{1/b-\sigma}} \quad (\text{B.44})$$

$$c_1 = w \frac{\alpha}{1-\alpha} d_w l_1 \quad (\text{B.45})$$

Across periods Several equilibrium conditions are informative about how parental investments relate to each other over time. For example, Eq. (B.39) from the general setup can be used to show how the ratio of early to late direct investments depends on the ratio of investments x_t and e_t (dividing the expressions for both periods):

$$\frac{x_1}{x_2} = \left[\frac{\underline{G} + \kappa w h_1 + e_1}{\underline{G} + \kappa w h_1 + e_2} \right]^{\frac{1-b\sigma}{1-a\sigma}} \quad (\text{B.46})$$

Eq. (B.42) shows that while consumption is equal across the two periods for all parents, leisure is not necessarily equal. Parents consume the same amount of leisure in both periods only if $d_w = 1$, that is if $w = 1$. The derivative of d_w with respect to w is positive,⁴¹ thus the ratio of l_2/l_1 is *increasing* in w , therefore it is increasing in parental quality. High earning parents have less leisure early relative to later than low-earning parents. That does not mean that they have lower *levels* than low-earning parents.

⁴¹Because if $\kappa < 1$, and unless $\kappa w = 1$, $\frac{\partial d_w}{\partial w} = \frac{(1-\kappa)(1+\beta\kappa w)}{(1-\kappa w)^2} = \frac{\pm}{+} > 0$.

Within periods Other conditions relate different choice variables within periods, such as Eqs. (B.41) and (B.45), but also Eq. (B.39).

A full expression of children's skills in period 2 can be obtained if we further align the functional forms of investments in private and public by setting $a = b$. Then, the full production function can be expressed as:

$$\theta_2 = \left\{ \gamma^2 \theta_0^\phi + \gamma(1 - \gamma) \left[H(\theta_P) x_1^a \right]^\phi + (1 - \gamma) \left[H(\theta_P) x_2^a \right]^\phi \right\}^{1/\phi} \quad (\text{B.47})$$

where $H(\theta_P) = \theta_P^a \pi^{\frac{1}{\sigma}} \left[1 + \frac{\pi}{(1-\pi)} \frac{1}{a\sigma-1} \theta_P^{\frac{a\sigma}{a\sigma-1}} \right]^{1/\sigma}$ is an *investment multiplier* capturing that parents' investments become more effective as their skills increase in the first term in the brackets and in the second term that parents' investment choices depend on whether investments at home or in an institutional setting are substitutes or complements.⁴² Thus, $H(\theta_P)$ captures the inequality in total investments in a given period for a given level of parental home investments x_t .

B.4 Effects of a shock to institutional investments (increase in \underline{G})

Our empirical setting changes \underline{G} randomly in period 1, say by the amount s . Parents who were treated then expect that total G in period 2 becomes $G_2 = g((\underline{G} + s) + \kappa w h_1 + e_2)$. This change in the framework within which parents make decisions will cause treated parents to re-optimize their time allocation for the second period (they cannot re-allocate debt, which is repaid in period 2). The relevant equilibrium conditions involving first-order conditions for second-period time variables are Eqs. (B.39) and (B.41). Eq. (B.41), together with the time and budget constraints for period 2, becomes the following:

$$h_2 = \alpha(1 - x_2 - e_2) + (1 - \alpha)(h_1 \kappa + \frac{1}{w\beta} B) \quad (\text{B.48})$$

⁴² $\frac{\partial H}{\partial \theta_P} > 0$ as long as $1 + \frac{a\sigma}{a\sigma-1} \theta_P^{\frac{a\sigma}{a\sigma-1}} > 0$ which it will be in all but a few special cases where θ_P close to 0 and $a\sigma$ is close to 1.

Eq. (B.39) in a convenient format lets us look at comparative statics:

$$x_2^{1-a\sigma} = \theta_P \frac{a}{b} \frac{\pi}{1-\pi} ((\underline{G} + s) + \kappa wh_1 + e_2)^{1-b\sigma} \quad (\text{B.49})$$

When the right hand side of Eq. (B.49) increases by s for the treated group, the adjustment back to optimality can happen through a *reduction* in e_2 and/or an *increase* in x_2 on the left hand side. At this point, the magnitudes of these changes cannot be determined yet, but we can study the ratio of possible changes that yield optimality.

$$\frac{\Delta x_2}{\Delta e_2 + s} = \frac{1 - b\sigma}{1 - a\sigma} \frac{a}{b} \frac{\pi}{1 - \pi} (\underline{G} + \kappa wh_1 + e_2)^{-b\sigma} x_2^{a\sigma} \quad (\text{B.50})$$

The ratio of the change in x_2 relative to the combined change in e_2 and the random shock s will be *large* when parents are already investing a lot directly (high level of x_2), when the level of e_2 is low, or when wh_1 is low. In those cases, any remaining increase in G (if parents do *not* offset the increased s by enough decreased e_2) would have to be compensated by large increases in x_2 , because these parents are already at the part of the production function where the marginal productivity of additional increases in x_2 is relatively low. A large increase in x_2 risks being costly in terms of leisure or work time, which would risk reducing utility. Thus, for these parents it is likely more advantageous to have a high ratio on the left hand side of Eq. (B.50) through a small denominator - that is, offsetting the positive s through a greater reduction in e_2 .

We now return to the more general model for a brief description of the intuition from a shock to public investments. Figure B.2 illustrates the impact of an increase in public investments \underline{G} on parents' investment decision. As \underline{G} increases through the intervention's increase in \underline{G} , this affects the marginal product of all other inputs in institutional investments G , exemplified by the change in Figure B.2a (here assuming a concave production function for illustrative purposes).

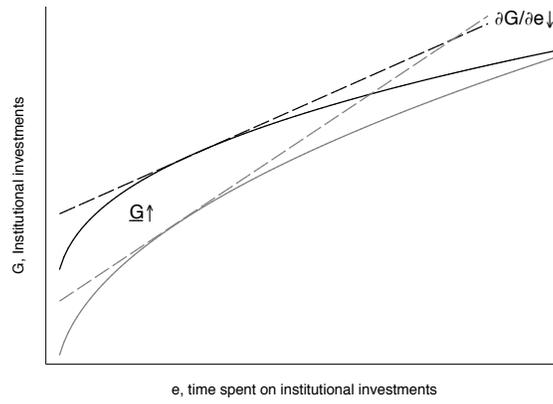
The equilibrium condition Equation (B.9) is thereby possibly violated (as several terms change), begging adjustments to parents' investment decisions, which are illustrated in Fig-

ures B.2b and B.2c. Parents can, for example, respond to the decreasing marginal product of time input in institutional investments, by increasing time spent on home investments (B.2b), thereby decreasing the marginal product of time spent on home investments accordingly – or they can reduce time spent on institutional investments (B.2c).

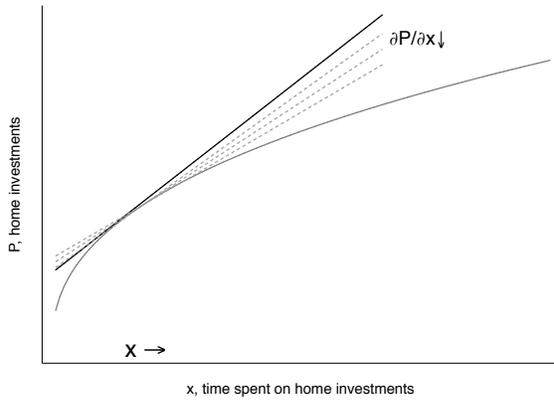
The direct impact of the randomized increase in \underline{G} and the subsequent parental adjustments will, therefore, depend i) on the (sign of the) elasticity of substitution between home and institutional investments, and ii) the production functions linking home and institutional investments to the time inputs. *This is the key insight we use to identify the sign of the elasticity of substitution from an RCT increasing \underline{G} .*

Figure B.2: Impact of increasing \underline{G}

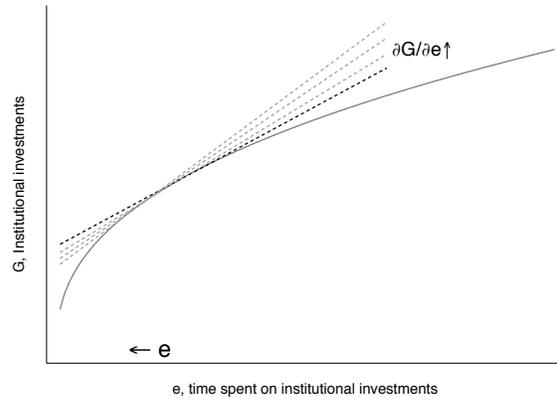
a) Impact of increase in institutional investments G through higher \underline{G}



b) Response through x



c) Response through e



Note: The figure illustrates the change following an increase in public investments \underline{G} . a) illustrates the direct impact of an increase in \underline{G} on the marginal productivity of institutional investments. b) and c) illustrate how parents can adjust either time spent at home x (increase) or time spent on institutional sorting e (decrease) to satisfy the equilibrium condition from Equation (B.9).

B.5 Determining the Progressivity of an Increase in \underline{G}

The model informs us also about whether an increase in the public baseline investments \underline{G} benefits highly educated parents more or less than less educated parents—in other words, whether the intervention is progressive or regressive. We perform this analysis using the version of the model with all functional form assumptions for utilities and residential choice in period 1 only, for convenience (see Section B.3).

Seen from the perspective of the 2nd period (with respect to discounting), the change in parents' utility from increasing \underline{G} in period 1 is:⁴³

$$\frac{dU(c_1, c_2, l_1, l_2, \theta_2)}{d\underline{G}} = \frac{\partial u(c_2)}{\partial \underline{G}} + \frac{\partial u(l_2)}{\partial \underline{G}} + \beta \frac{dV(\theta_2)}{d\underline{G}}$$

Observing Eq. (B.41), and by definition $\partial U/\partial l = (1 - \alpha)/l$, this expands and then simplifies to

$$\begin{aligned} \frac{dU(c_1, c_2, l_1, l_2, \theta_2)}{d\underline{G}} &= 1/w \frac{\partial u_2}{\partial l_2} \frac{\partial (w \frac{\alpha}{1-\alpha} l_2)}{\partial \underline{G}} + \frac{\partial u_2}{\partial l_2} \frac{\partial l_2}{\partial \underline{G}} + \beta \frac{dV(\theta_2)}{d\underline{G}} \\ &= \frac{1}{l_2} \frac{\partial l_2}{\partial \underline{G}} + \beta \frac{1}{\theta_2} \frac{d\theta_2}{d\underline{G}} \end{aligned} \quad (\text{B.51})$$

Combining Eqs. (B.19) and (B.41) and the time budget constraint for period 2, we know that $l_2 = (1 - \alpha)(1 - x_2 - e_2 - \kappa h_1)$, which can be further used to derive Eq. (B.52). Then, continue with Eq. (B.8) and expand the term $d\theta_2/d\underline{G}$:

$$\frac{dU(c_1, c_2, l_1, l_2, \theta_2)}{d\underline{G}} = - (1 - \alpha) \frac{1}{l_2} \left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right) + \beta \frac{1}{\theta_2} \frac{d\theta_2}{d\underline{G}} \quad (\text{B.52})$$

$$\begin{aligned} &= (1 - \alpha) \frac{1}{l_2} (-1) \left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right) + \beta \frac{1}{\theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial \underline{G}} + \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2} \left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right) \\ &= \beta \frac{1}{\theta_2} \frac{\partial \theta_2}{\partial \theta_1} \frac{\partial \theta_1}{\partial \underline{G}} + \left(\frac{\partial x_2}{\partial \underline{G}} + \frac{\partial e_2}{\partial \underline{G}} \right) \left[\beta \frac{\partial \theta_2}{\partial I_2} \frac{\partial I_2}{\partial P_2} \frac{\partial P_2}{\partial x_2} - (1 - \alpha) \frac{1}{l_2} \right] \end{aligned} \quad (\text{B.53})$$

⁴³Note that the notation of \underline{G} can be confusing because it lacks a time subscript. In all following, however, it should be considered as happening *only* in period 1.

C Data appendix

C.1 The Survey

In late April 2017, an invitation to participate in a survey was sent to all parents with children who had participated in the intervention. The invitation was sent via the personalized secure email *e-Boks*⁴⁴ to minimize non-response and ensure that all parents received the invitation. **All** Danes have such an email inbox in *e-Boks* and use this to receive (and send) official communications, such as from employers or public sector officials, on everything from children’s medical visits, preschool and school enrolment, reception of public transfers, tax records, etc.

The letter is presented below.⁴⁵

⁴⁴See <https://www.e-boks.com/danmark/en/what-is-e-boks/>.

⁴⁵In English:

Dear Parents to [Child]

We are a group of researchers who are studying the environments that help children flourish and provide them with the best possible beginning of their life.

Your child’s daycare has been part of a project focussing on children’s language development, and you were in this context asked to participate in a survey a couple of years ago.

The interplay between different activities in a child’s day

We would like to request your assistance by filling our a similar questionnaire. The questionnaire ask questions relating to your everyday activities, habits, and how your view your child’s everyday. We would like to ask you this to improve our understanding of how children’s everyday activities in- and outside the home environment are linked.

The questionnaire can be found by following this link: LINK

It will at most take 15 minutes to respond to the questionnaire, and you will – upon completion – participate in a lottery with the possibility of winning an iPad. Lottery-participation is not conditional on having participated in the old survey.

The study has been approved by the Danish Data Authorities (National IRB board) and *all information is confidential and will be anonymized*.

We hope you will participate in the survey and thereby provide an important contribution to the understanding of the early childhood of all children. If you have any questions, please let us know by writing to: startpaalivet econ.au.dk.

Den 21. april 2017

Kære forældre til [barns navn]

Vi er en gruppe af forskere, der er i færd med at undersøge, hvordan børn får de bedste betingelser til at udvikle sig under opvæksten og den bedst mulige start på livet.

Jeres barns dagtilbud har tidligere været med i et projekt med fokus på børns sproglige udvikling, og i den forbindelse har I for ca. 2 [3, 4] år siden fået tilsendt et spørgeskema.

Samspillet mellem aktiviteter i børns hverdag

Vi vil nu bede jer om at hjælpe os igen ved at udfylde et lignende spørgeskema. Det handler om jeres hjem, vaner og opfattelse af jeres barns hverdag. Vi vil gerne spørge jer om dette for bedre at forstå samspillet mellem de aktiviteter, som børn laver i deres hverdag både ude og hjemme.

Spørgeskemaet findes på dette link: www.spørgeskema.dk.

Det tager kun ca. 15 minutter at besvare spørgeskemaet, og når I besvarer, deltager I samtidig i en lodtrækning om en iPad. I behøver ikke have besvaret det foregående spørgeskema for ca. 2 [3, 4] år siden for at besvare dette.

Undersøgelsen er godkendt af Datatilsynet, og *alle oplysninger behandles anonymt og fortroligt*.

Vi håber, at I kan hjælpe os, og derved give et vigtigt bidrag til at øge forståelsen af, hvordan samfundet bedst muligt kan hjælpe alle børn på vej i deres tidlige år. Hvis I har spørgsmål til projektet, kan I kontakte os på startpaalivet@econ.au.dk.

Venlig hilsen

Dorthe Bleses (Professor, TrygFondens Børneforskningscenter på Aarhus Universitet)

Rasmus Landersø (Seniorforsker, ROCKWOOL Fonden)

Following the letter, two reminders were sent to non-respondents, and later non-respondents were contacted by phone. The survey items are listed below. Some questions contain different phrasing for preschool and primary school students (such as “When do you pick up your child from school/preschool.”) Here, we only give one version for brevity, and note in parentheses the school version when it differs.

Sincerely,

Dorthe Bleses (Professor, TrygFonden’s Centre for Child Research)

Rasmus Landersø (Rasmus Landersø, Senior Research, The Rockwool Foundation Research Unit)

In these first questions we will ask about your thoughts and concerns about your child's day, and what your child is doing in kindergarten. If you are unsure of the answer to a question, please share your best judgment.

1. How many times a week are you informed by the staff/teachers about what your child has done during the day?
2. How satisfied are you with the language support your child receives in preschool (school)?

How much do you agree with the following statements?

3. I know how often my child is being read with in preschool (school).
4. I would like to know more about how often my child is being read to in preschool (school).
5. One of the reasons I read to my child is to support my child's language learning.
6. I think the amount my child is being read to in preschool (school) is not sufficient.
7. If they read less in preschool (school), I would read more with my child.
8. I think it is boring or difficult to read to my child.
9. I enjoy reading to my child.
10. I am often too busy or too tired to read to my child.
11. I do a lot to teach my child to focus, concentrate, and complete a task.
12. One of the reasons I support my child's ability to focus, concentrate, and complete a task, is because there is not enough focus on it in preschool (school).
13. When I play or read with my child, it is important that we finish before we stop or start new things.
14. I would like my child to receive more help to develop his ability to concentrate on a task.
 - If strongly/mildly agree:
 - (a) I would like my child to receive more help in order to develop as much as possible his/her ability to concentrate on a task.
 - (b) I would like my child to receive more help in order to not lose ground relative to his/her peers' ability to concentrate on a task.
 - If strongly/mildly disagree:
 - (c) My child does not need more help because my child is already good at concentrating on a task.
 - (d) My child does not need more help because my child's ability to concentrate is age-appropriate.
15. I feel that my child's language skills are better than the majority of his/her peers.
16. I feel that my child's language skills are weaker than the majority of his/her peers.
17. I would like my child to receive more help to develop his/her language skills.

- If strongly/mildly agree:
 - (a) I would like my child to receive more help in order to develop his/her language as much as possible.
 - (b) I would like my child to receive more help in order not to lose ground relative to his/her peers' language skills.
- If strongly/mildly disagree:
 - (c) My child does not need more help because his/her language skills are already good.
 - (d) My child does not need more help because my child's language skills are age-appropriate.

Now we ask you about your life and what you are doing with your child.

18. At what time does your child begin her/his day in preschool (school) on a typical day?
19. At what time is your child typically picked up from preschool (school)?
20. How many hours do you typically work per week?
21. How much time do you typically spend in commute to/from work?
22. How many books do you have in your home (including fiction, non-fiction, cookbooks, religious books, etc. but excluding children's books)?
23. How many children's books do you have in your home?
24. In the last week, how many times did you read books, newspapers, e-books, magazines, religious texts, texts on the tablet (eg iPad) or computer at your leisure?
25. During the last week, how often did you and your child do everyday activities together, such as cooking?
26. How often did you talk with your child about what they have done in preschool (school) in the last week?
27. How many times during the last month have you talked to your child about how he/she is doing generally?
28. How many times during the last month have you talked to your child about how it is going academically?
29. How many of your child's friends from preschool do you know by name?
30. In the last week, how often did you encourage or help your child to talk about letters (words and spelling)?
31. In the last week, how often did you encourage or help your child to talk about numbers, shapes, patterns (numbers, magnitudes, nature)?
32. How many times last week has your child been read to (or read with) at home?
33. (If your child can read, how often in the past week have you sat with your child while it read to you?)

34. (How many times last week have you or your child read, not counting schoolwork?)
35. How often did you sing or rhyme with your child last week?

In the next questions we will ask about your views about your child's development. There are no 'right' or 'wrong' answers. How much do you agree with the following statements?

36. As a parent, I have a big influence on how my child is going to learn to read, write and count.
37. My child is not old enough to acquire skills that are linked to read and write. (only preschool)
38. My child's ability to learn to read, count and calculate the intrinsic and will never change.
39. My child can always improve its ability to learn to read and count, no matter how old he / she is.
40. After a certain time my child will no longer be able to improve its ability to learn to read, count and calculate.
41. I can affect my child's ability to focus on completing a task.
42. There is not much I as a parent can change if my child has a harder time concentrating than other children.

In the next questions we ask about your assessment of how important it was that your child participated in the daycare intervention. (Only given to parents whose children took part in the intervention in any of the three programs)

43. My child's development was strengthened by the day-care participation in the intervention.
44. The participation of my day-care center in this intervention became important for the activities I do with my child at home.

C.2 Survey Response

The survey-response rate was 60%, and in the main results we do also include non-respondents (as we have information on all the remaining key variables from the initial post-trial test scores and subsequent full population register data). The tables below compare characteristics of respondents and non-respondents.

Table C.1 presents estimation results from regressions of survey-response (0/1) on baseline characteristics for the control and treatment groups in columns 1 and 2, respectively. The two columns show that survey response cannot be considered random. As would be expected, respondents are on average older, have completed more years of schooling, have a higher family income, and have children that score higher in language tests. However, when testing

for treatment–control differences in the estimates, column 3 shows that only father’s age is significant. Moreover, there are no significant differences in response rates between the two groups.

Next, Table A.1 compares treatment effects across different sample restrictions. The columns labeled “unrestricted” present estimates for the full sample considered in the main analysis. The columns labeled “panel DNT” show estimates for those who have reached grade 2, and the columns labeled “panel + survey” show the results for those who have reached grade 2 and whose parents have responded to the survey. The table shows that treatment-control differences are almost identical across the different specifications. Thus, the only difference across the specifications and sampling is the power of our results.

C.3 Data Construction

This section describes the data construction. The first step was to collect the data from the intervention (see Section 3.1) and transfer it to Statistics Denmark. Here, the data was anonymized (i.e. all social security numbers were changed to anonymized unique *pnr*-numbers) with a code facilitating the link between the intervention data and the register data using the anonymized *pnr*-numbers. A similar procedure was conducted once the survey data had been collected.

The register data encompasses the entire population of Denmark from 1980 to the present with family identifiers (parent identifiers *pnr_m*, *pnr_f* and household identifiers *familie-id*), allowing us to link the children from the intervention to their parents. From the demographic register we also identify the children’s country of origin (we limit the sample to those with at least one native parent), date of birth, and home addresses (again anonymized). We also link the children to the daycare register (DAGI) and educational register (UDDA). These data also include unique preschool and school identifiers (institution-numbers) allowing us to identify the institutions the children attend along with the peers at the same institutions.

Table C.1: Determinants of response to follow-up survey

	(1) Nonresp.	(2) Respondents	(3) Diff Resp.-Nonresp.
Treatment	0.481 (0.500)	0.513 (0.500)	0.032 (0.021)
Pre-trial Test	-0.122 (0.994)	0.081 (1.003)	0.202*** (0.043)
Post-trial Test	0.496 (0.963)	0.677 (0.940)	0.181*** (0.041)
Age 1-9/17	8.255*** (1.036)	8.274*** (1.026)	0.019 (0.044)
Father's age, 1/9-17	41.870*** (5.792)	42.407*** (5.852)	0.538* (0.249)
Father's age at child's birth	33.192*** (5.754)	33.679*** (5.805)	0.487+ (0.251)
Father years of schooling	13.570*** (2.399)	14.124*** (2.410)	0.554*** (0.103)
Mother's age, 1/9-17	39.408*** (5.202)	40.134*** (4.916)	0.726*** (0.215)
Mother's age at child's birth	30.657*** (5.083)	31.375*** (4.802)	0.718*** (0.210)
Mother years of schooling	13.708*** (2.571)	14.431*** (2.365)	0.723*** (0.105)
Household wage income 2017, \$1,000	94.675 (65.100)	102.973 (67.916)	8.298** (2.853)
N	903	1,397	2,300

Note: Columns 1 and 2 show descriptive characteristics according to who responded to the follow-up survey (mean and standard deviation). Column 3 tests the difference between the two, with standard errors in parentheses. +(p < 0.1), * (p < 0.05), ** (p < 0.01), *** (p < 0.001).

C.4 Background Characteristics and Outcomes

The pnr-numbers allow us to link the children to the National Birth Register and obtain information on their birth weight, gestation length, Apgar score, and mothers' weight at the time of pregnancy. Using the parental identifiers, we also include information on parents' completed education from the educational register, employment status from the labor market register (RAS), and household income from the income register (based on tax authorities' information).

Child outcomes We study two child-outcomes: post-trial language test scores and grade 2 language test scores. The pre- and post-trial tests are constructed from 50 items relating to sound discrimination, rhymes, word-segmentation, and letter identification. We standardize the tests (mean zero, std. dev. 1) relative to the control group.

The grade 2 test scores are part of the compulsory national tests from grade 2 through 8 (with language tests in grades 2, 4, 6, 8). The tests focus on three underlying constructs: Reading comprehension, decoding, and language comprehension, and they take place near the end of the school year. The tests are performed on computers using an adaptive system in which questions are determined by the student's performance earlier in the test. The test is scored electronically without teacher input. Following [Sievertsen et al. \(2016\)](#) and [Beuchert and Nandrup \(2018\)](#), we standardize these three individual scores, take the simple average, and re-standardize them within year.

Parent outcomes We construct *parental investments* from a factor analysis with 26 items that describe parental activities and opinions. After extensive exploratory factor analysis, we perform a principal-component analysis with the number of factors limited to five, adding an oblique promax rotation with power 3. The estimates are reported in Table C.2. From these estimates, we predict five factor scores with Bartlett scores. The six statements/questions that load on the parental investment factor have six potential answers ranging from, for

example, highly disagree to highly agree. We assign these answers values 1 to 6 in the factor analysis. Note that if we predict a parental investment factor score from a factor analysis that uses exclusively the parental investment items (instead of the full list of 26 as in Table C.2, the results are very similar. These two versions of a parental investment factor are correlated at .97.

Items that mainly load on parental investment factor

- How many times last week has your child been read to (or read with) at home?
- If your child can read, how often in the past week have you sat with your child while it read to you?
- How many times last week have you or your child read, not counting schoolwork?
- I think it is boring or difficult to read for my child.
- I enjoy reading for my child.
- I am often too busy or too tired to read to my child.

Table C.2: Factor Loading Matrix of Parental Activities and Opinions

	Neg.Pub Eval	Parental Inv.	Growth Mindset	Home Capital	Noncog Important
How many times last week has your child been read to (or read with) at home?	0.075	0.709	-0.094	0.055	0.244
If your child can read, how often in the past week have you sat with your child ...	0.080	0.528	-0.108	-0.160	0.391
How many times last week have you or your child read, not counting schoolwork?	0.055	0.585	-0.084	0.190	0.159
I think it is boring or difficult to read for my child.	0.063	-0.620	-0.154	-0.020	0.155
I enjoy reading for my child.	-0.004	0.643	0.146	0.033	-0.068
I am often too busy or too tired to read to my child.	0.074	-0.696	0.037	0.044	-0.057
As a parent, I have a big influence on how my child is going to learn to read, ...	-0.003	0.092	0.566	-0.030	0.169
My child's ability to learn to read, count and calculate are intrinsic ...	-0.063	0.059	-0.568	-0.020	0.053
My child can always improve its ability to learn to read and count, no matter ...	0.055	-0.081	0.670	-0.030	0.168
After a certain time my child will no longer be able to improve its ability to ...	-0.010	0.110	-0.615	-0.057	0.043
I can affect my child's ability to focus on completing a task.	-0.005	0.026	0.727	-0.003	0.090
There is not much I can change if my child has a harder time concentrating.	0.048	-0.046	-0.672	-0.025	0.034
I do a lot to teach my child to focus, concentrate, and complete a task.	-0.056	0.086	0.166	-0.169	0.544
When I play or read with my child, it is important to finish before we stop ...	0.152	0.049	0.090	-0.195	0.375
During the last week, how often did you and your child do everyday activities ...	-0.077	0.039	-0.009	0.293	0.490
How often did you talk with your child about what they have done in preschool ...	-0.100	0.113	0.047	0.001	0.622
How many times during the last month have you talked to your child ...	-0.028	0.035	0.121	0.079	0.493
I think the amount my child is being read to in preschool(school) is not sufficient.	0.678	-0.066	0.008	0.069	0.011
I would like my child to receive more help to develop his/her language.	0.679	-0.084	-0.032	-0.009	0.120
How satisfied are you with the quantity of language support your child receives?	-0.787	-0.152	-0.038	0.010	0.293
How satisfied are you with the quality of language support your child receives?	-0.822	-0.149	-0.075	-0.029	0.276
One of the reasons I support my child's ability to focus, concentrate, ...	0.667	-0.098	-0.005	0.020	0.173
I would like my child to receive more help to develop his ability to concentrate	0.610	-0.109	-0.094	-0.017	0.186
How many books do you have in your home?	0.048	0.000	0.023	0.845	-0.078
How many children's books do you have in your home?	0.025	0.117	-0.025	0.757	-0.013
In the last week, how many times did you read books, newspapers, e-books, ...?	-0.034	-0.050	0.039	0.612	0.221

Note: Factor loadings after PCA on all 26 items listed here, limited to 5 factors, with oblique promax rotation (power 3). $N = 1,336$. “Neg.Pub.Eval.” stands for a negative evaluation of the public investments by parents. “Parental Inv.” is the parental direct time investment factor used in the main analyses. “Growth Mindset” relates to how parents view their child’s potential to change, and their own potential to influence their child’s growth in both the cognitive and non-cognitive domains. “Home Capital” relates to the capital present in the home that could foster reading and language. “Noncog. Important” describes how important it is for parents to foster their child’s socio-emotional skills, in addition to reading and language.

Table C.3: Treatment-control differences in parental answers to the six main investment items

	(1) Control mean/sd	(2) Treatment mean/sd	(3) Treatment-Control coeff/std.err
How many times last week has your child been read to (...)?	3.772 (1.250)	3.954 (1.130)	0.169** (0.066)
If your child can read, how often in the past week have you sat (...)?	3.023 (1.338)	3.178 (1.308)	0.129+ (0.072)
How many times last week have you or your child read (...)?	3.357 (1.305)	3.341 (1.327)	-0.0460 (0.073)
I think it is boring or difficult to read for my child., reverse coded	5.304 (1.022)	5.394 (0.961)	0.109* (0.054)
I enjoy reading for my child.	5.279 (0.915)	5.333 (0.855)	0.034 (0.048)
I am often too busy or too tired to read to my child., reverse coded	3.867 (1.374)	4.046 (1.346)	0.142* (0.074)
Observations	750	828	

Note: Columns 1 and 2 show descriptive statistics of the individual items by whether or not parents were in the treatment or control groups of the intervention (mean and standard deviation). Column 3 shows the difference between the treatment and control groups (with standard errors in parentheses), indicating p-values of the null hypothesis of no differences Standard errors in parentheses. +(p < 0.1), * (p < 0.05), ** (p < 0.01), *** (p < 0.001).

Table C.3 shows how the overall treatment effect of the intervention on increasing parental investments originates in the different items.

Finally, we construct the variable on *hours worked* from survey responses to the following questions *At what time do you usually go to work?* and *At what time do you usually leave work?*

School quality Our measure of school quality is based on the average characteristics of the teachers employed in each school in Denmark. We use a unique link developed by Statis-

tics Denmark between all teachers (their pnr-numbers) and schools (institution-numbers) using employment records from the employer-employee match data to identify the full set of teachers employed at each school by January 1st from 2010-2016.

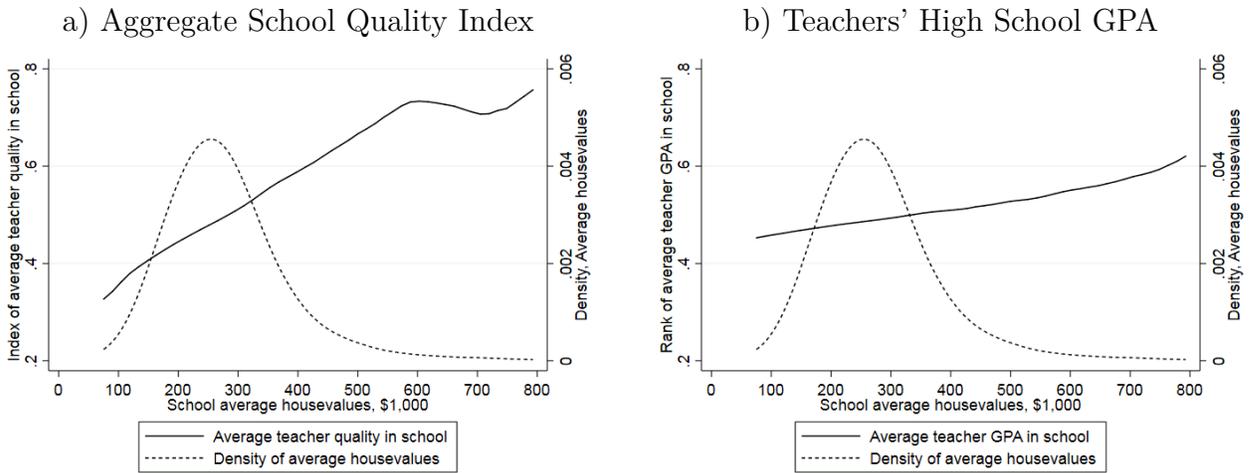
We link this data with the educational register, labor market register, and GPA from high school and teachers' college (UDG) to construct variables with each teacher's years of experience, tenure at a given school, unemployment spells and periods with sick leave, and GPA from high school and teachers' college.

The institution identifiers allow us to merge the aforementioned data with children's national test scores (see earlier paragraph). We obtain the predicted test scores from teacher characteristics by regressing the children's test scores on the school-by-year average teacher information. Finally, we rank schools from lowest to highest (0-1) by their predicted test score level.

Fig. C.1 shows school-average teacher characteristics by average property values in catchment areas. Fig. C.1a corresponds to Fig. A.3b. Fig. C.1b exemplifies how the underlying teacher characteristics vary across schools by plotting teacher high school GPAs against property values in school catchment areas.

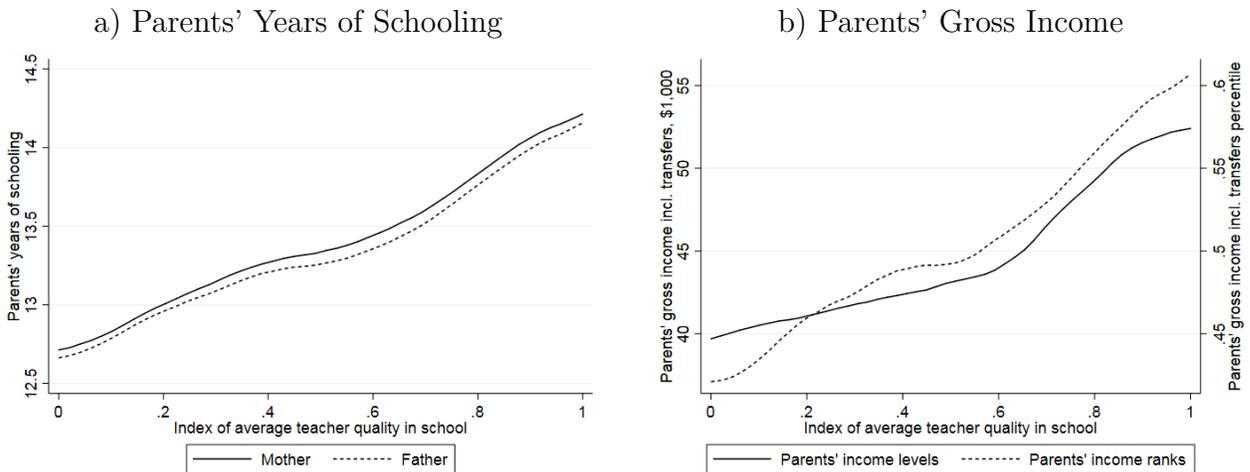
Fig. C.2 extends these associations by plotting parents' average years of schooling and gross (post-transfer, pre-tax) family income across the school quality index. Both Fig. C.1 and Fig. C.1 confirm the earlier findings of strong associations between school quality proxied by teacher characteristics and parental resources.

Figure C.1: Teacher Characteristics by Property Values



, **Note:** Note: The figure shows estimated school (teacher) quality in a) and teachers' average high school GPA rank (measured in the full population) by average housevalues of families with children in a given school.

Figure C.2: Parents' Education and Income by School Quality



, **Note:** Note: The figure shows parental characteristics, years of schooling in a) and gross income (market income plus transfer income) in b), by estimated school quality in the children's schools.